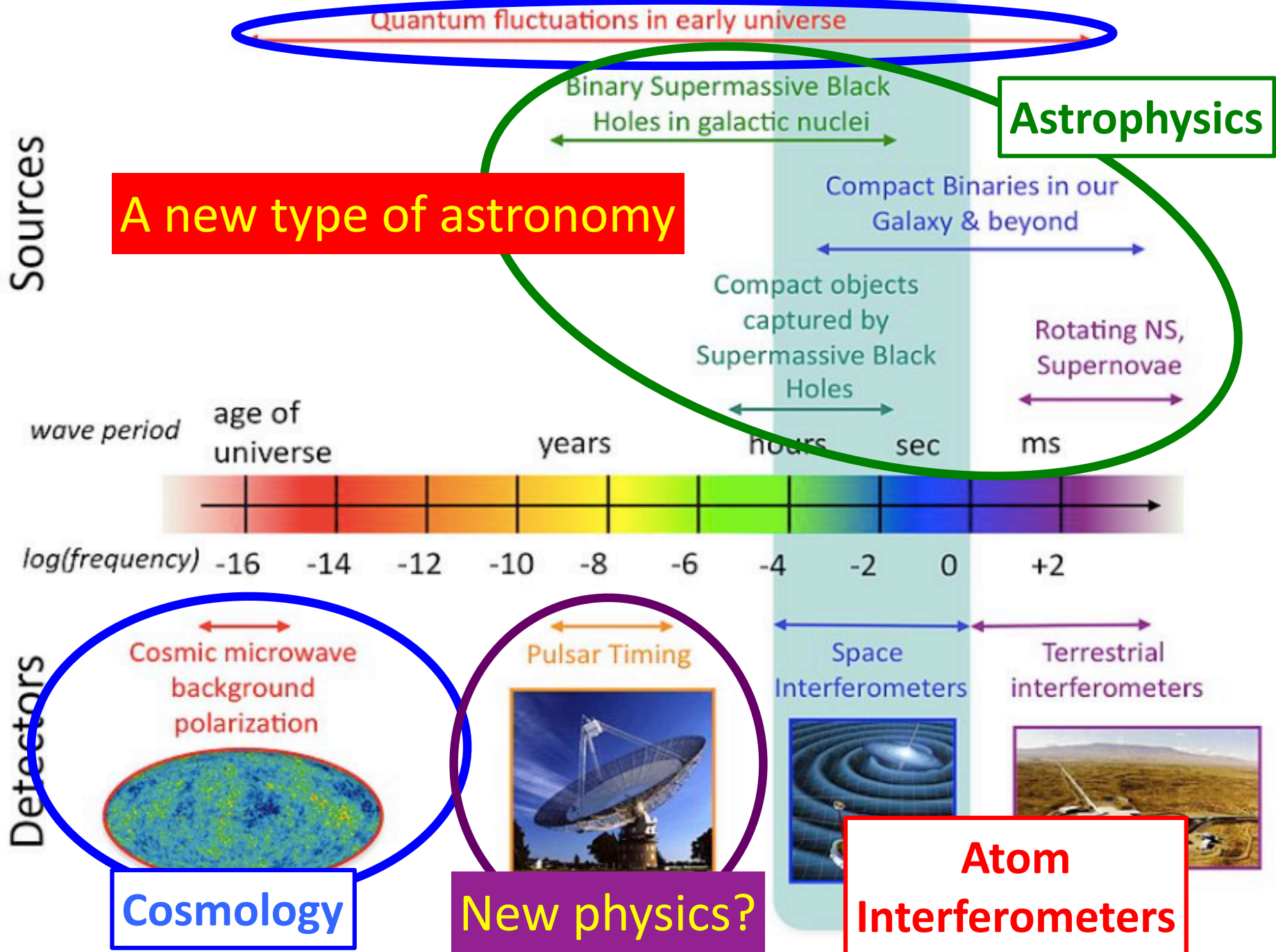


What is the source of the
gravitational waves
detected by NANOGrav
and other PTA
experiments?

John Ellis

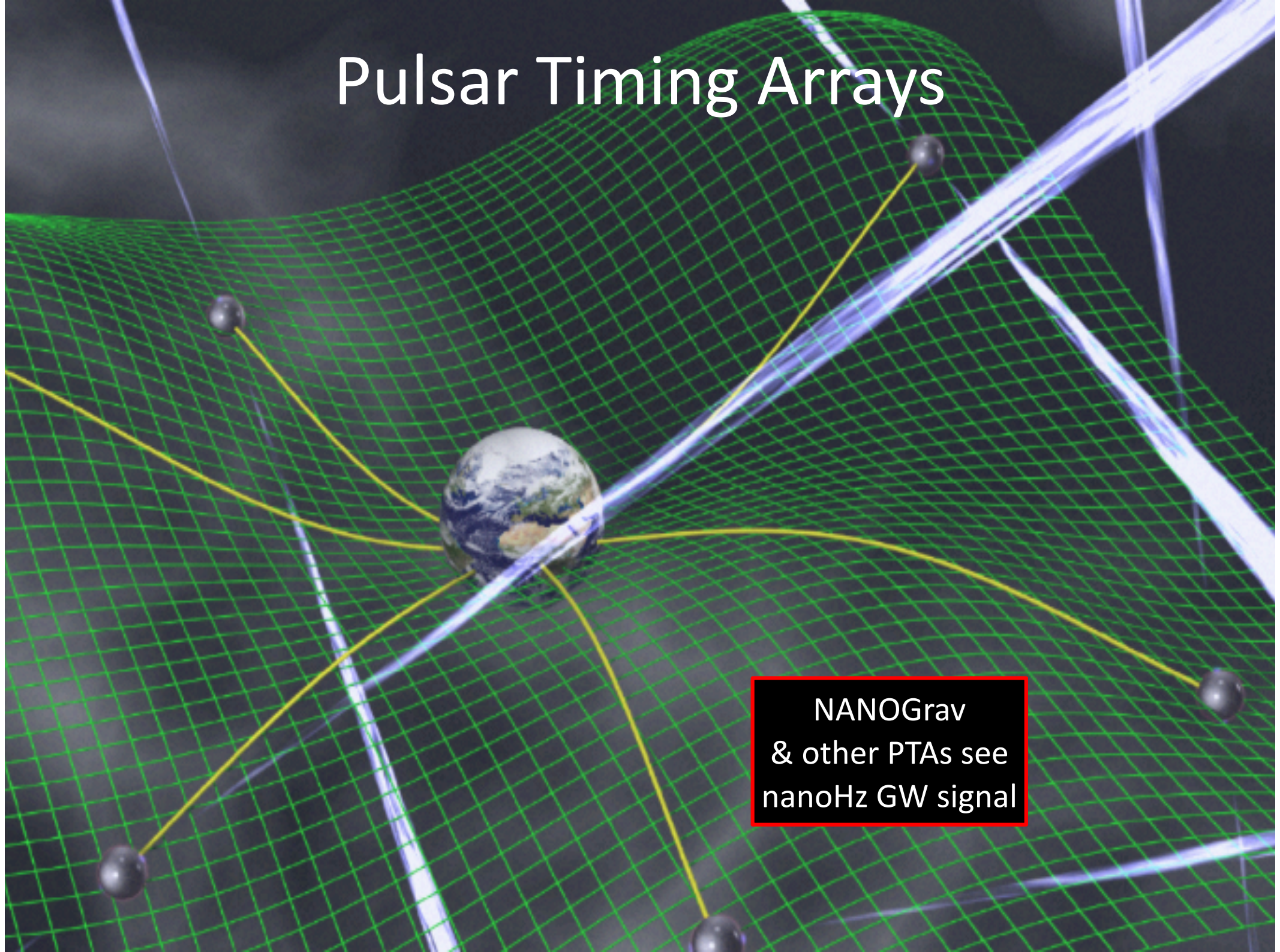
KING'S
College
LONDON

Gravitational Wave Spectrum



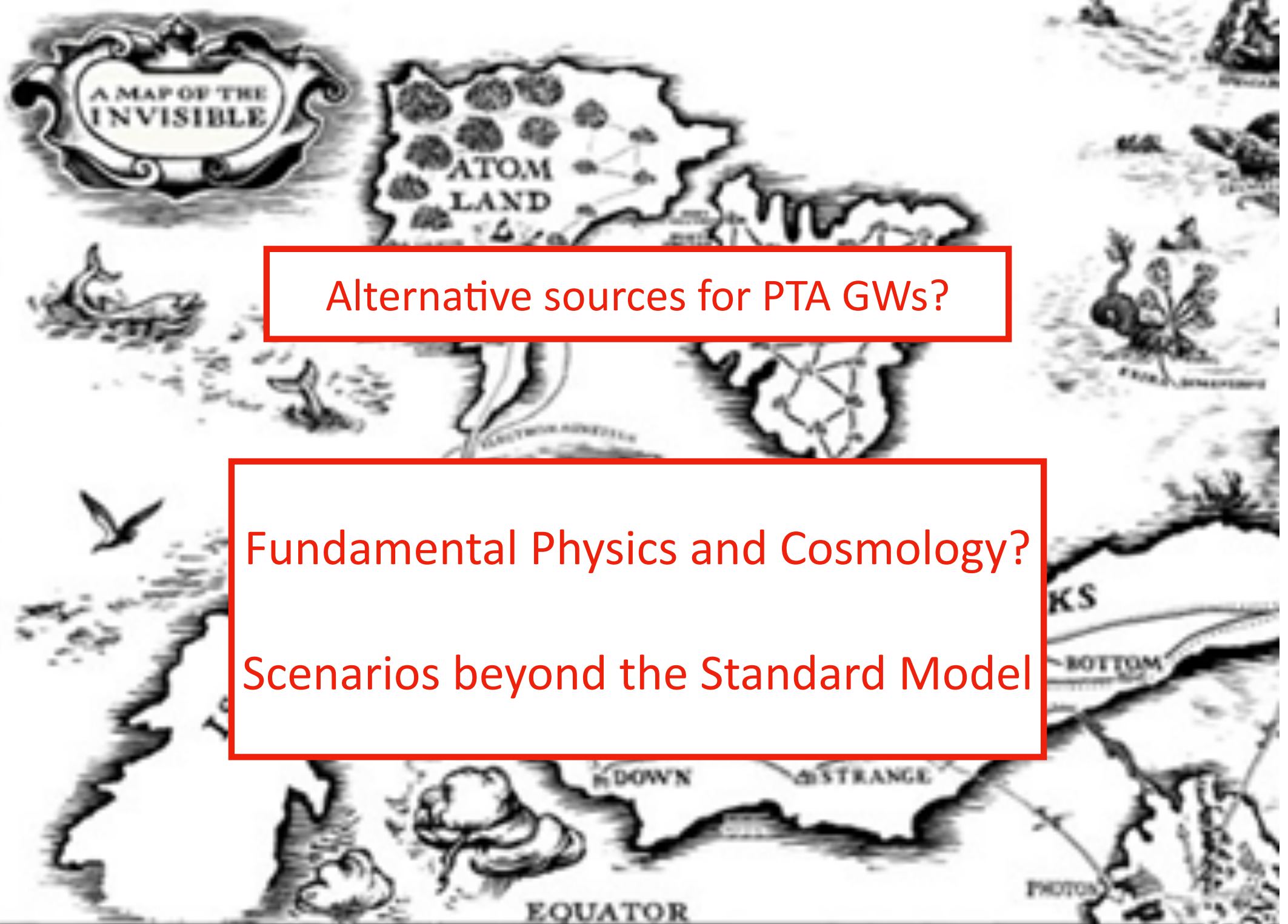
Pulsar Timing Arrays

NANOGrav
& other PTAs see
nanoHz GW signal



The Biggest Bangs since the Big Bang?

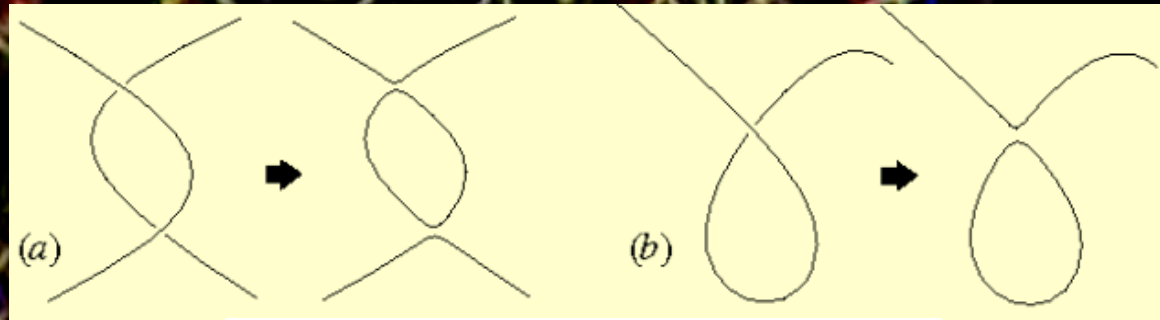




Alternative sources for PTA GWs?

Fundamental Physics and Cosmology?
Scenarios beyond the Standard Model

Cosmic Strings?



GW emission from string loops

Simulation of cosmic string network – Cambridge cosmology group

Cosmological Phase Transition?

Simulation of bubble collisions – D. Weir

Outline

- Supermassive black hole binaries?
- Analysis of NANOGrav PTA data
- Better fit if binaries interact with environment
- BSM scenarios:
 - Strings, phase transition, domain walls, 1st/2nd-order inflationary scenarios, axion
- **All fit NANOGrav data better than BH binaries!**

JE & Lewicki: arXiv:2009.06555;

JE, Fairbairn, Hütsi, Raidal, Urrutia, Vaskonen & Veermäe: arXiv:2301.13854;

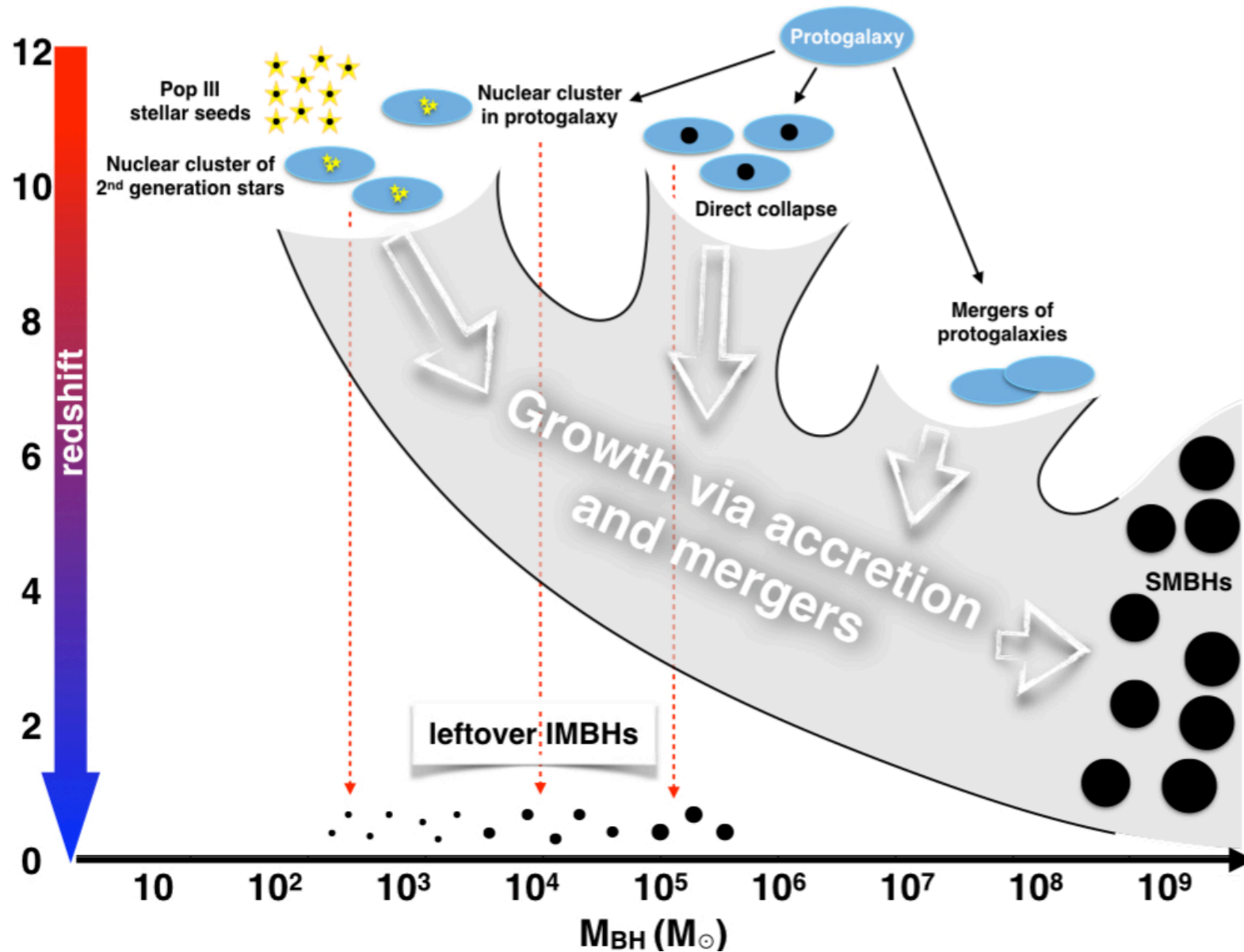
JE, Fairbairn, Hütsi, Raidal', Urrutia, Vaskonen & Veermäe: arXiv:2306.17021;

JE, Lewicki, Lin, & Vaskonen: arXiv:2306.17147;

JE, Fairbairn, Franciolini, Hütsi, Iovino, Lewicki, Urrutia, Vaskonen & Veermäe, arXiv:2308.08546

How to Make a Supermassive BH?

SMBHs from mergers of intermediate-mass BHs (IMBHs)?



BH Merger Rate Estimate

BH merger rate R_{BH}

$$\frac{dR_{\text{BH}}}{dm_1 dm_2} \approx p_{\text{BH}} \frac{dM_1}{dm_1} \frac{dM_2}{dm_2} \frac{dR_h}{dM_1 dM_2}$$

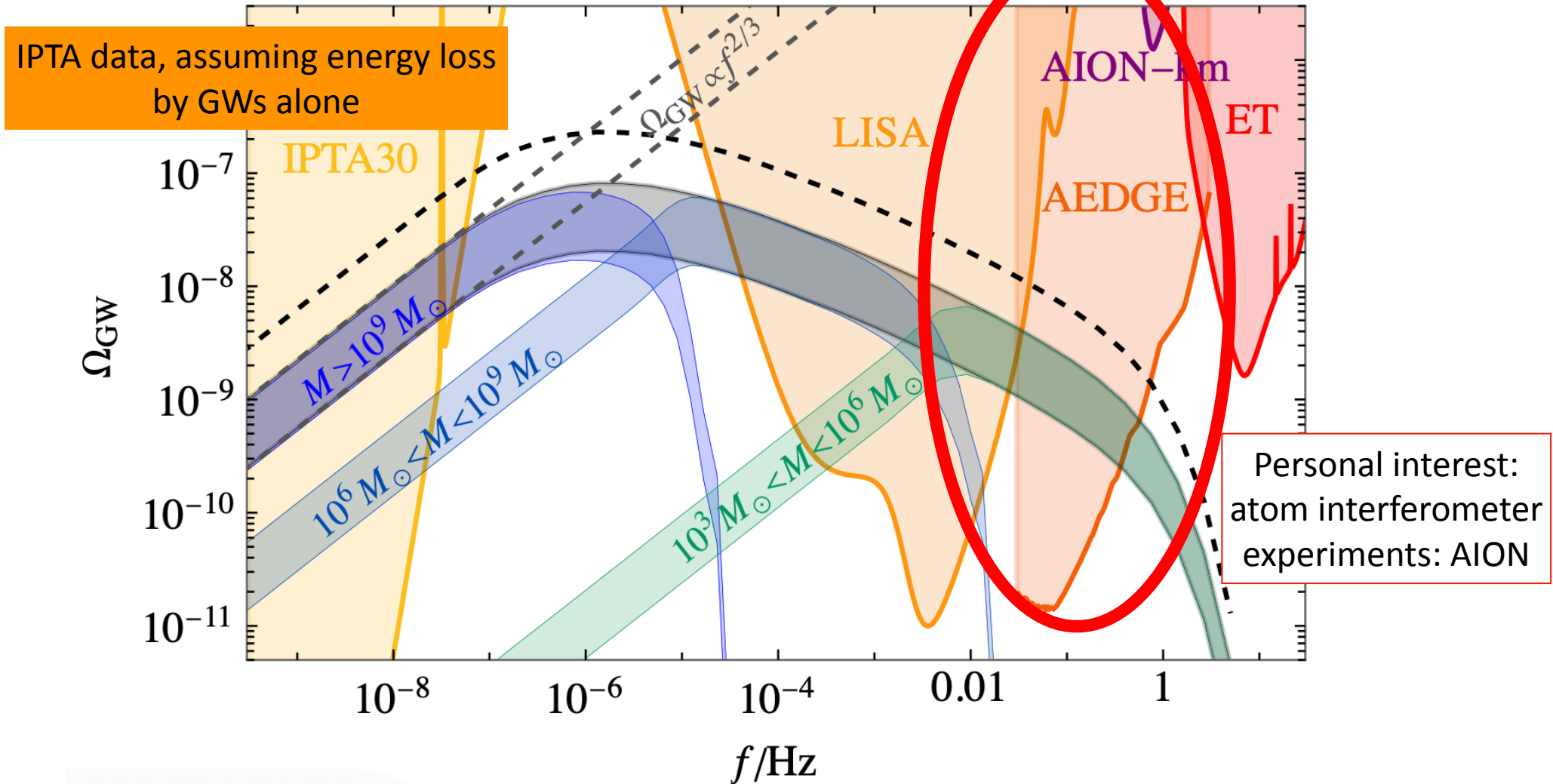
where R_h is halo merger rate calculated using Extended Press-Schechter formalism,

$$p_{\text{BH}} \equiv p_{\text{occ}}(m_1) p_{\text{occ}}(m_2) p_{\text{merg}}$$

is merger probability, and

strength of IPTA signal can be fitted by constant p_{BH}

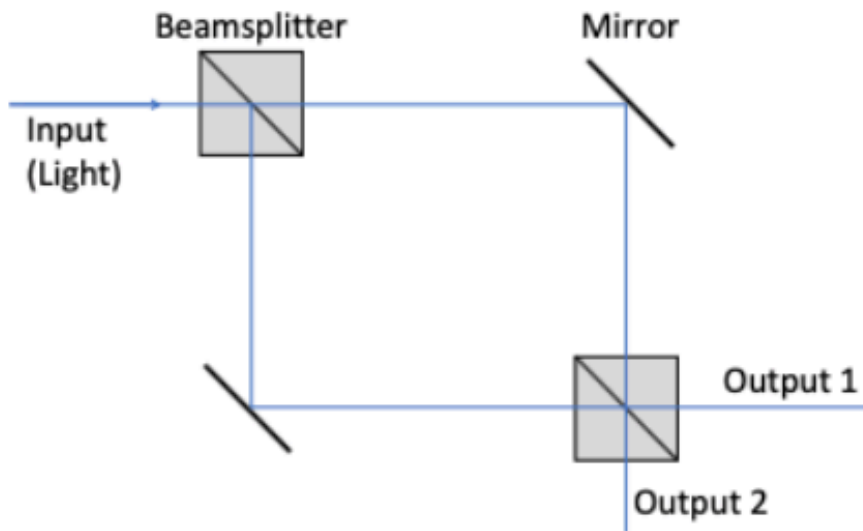
Stochastic GW Background from BH Mergers



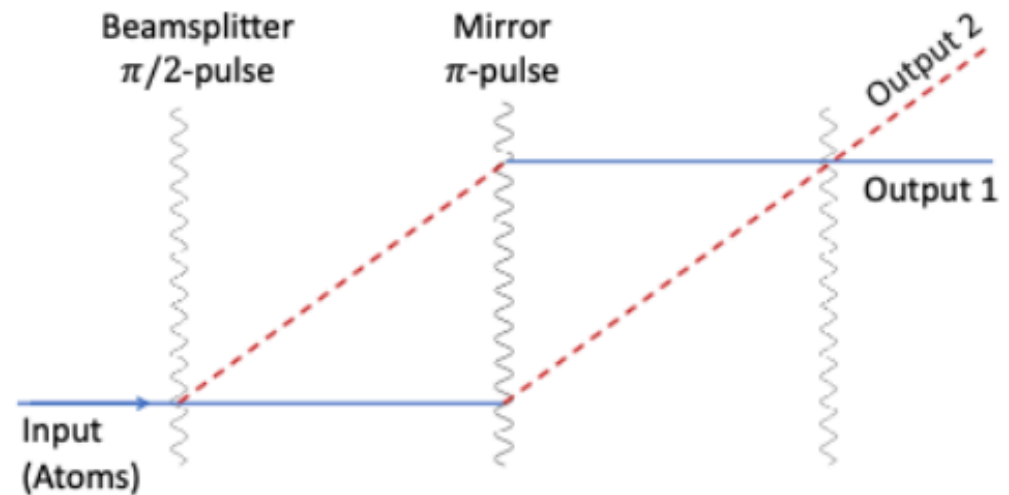
Black dashed line is maximum possible Ω_{GW} , i.e., $p_{\text{BH}} = 1$

Principle of Atom Interferometry

Mach-Zehnder Laser Interferometer

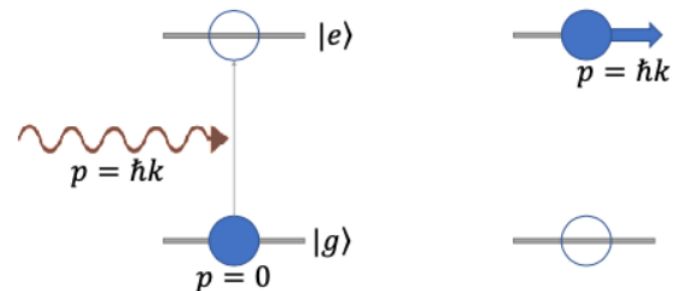


Atom Interferometer

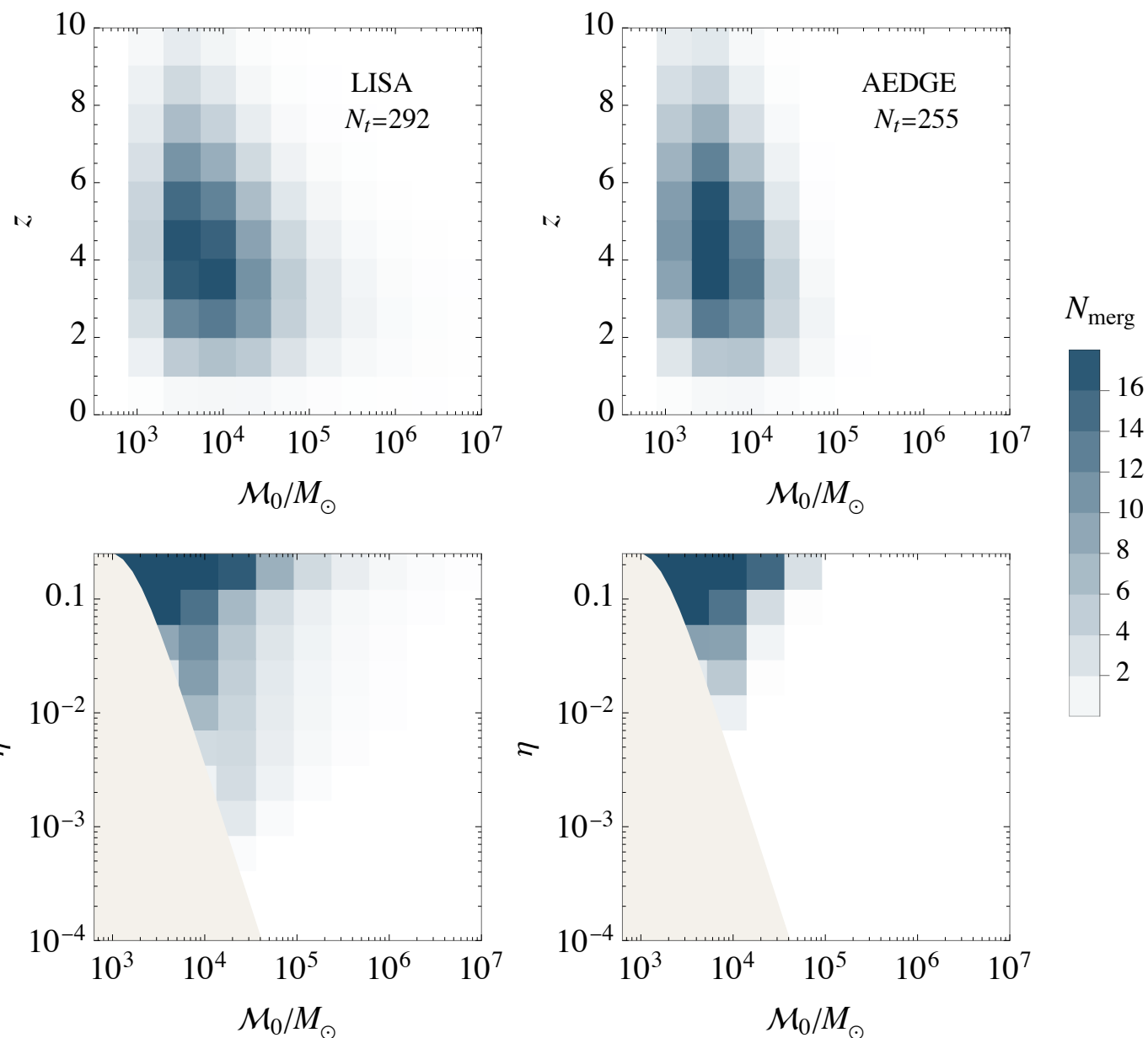


Laser excitation gives momentum kick to excited atom,
which follows separated space-time path

Interference between atoms following different paths



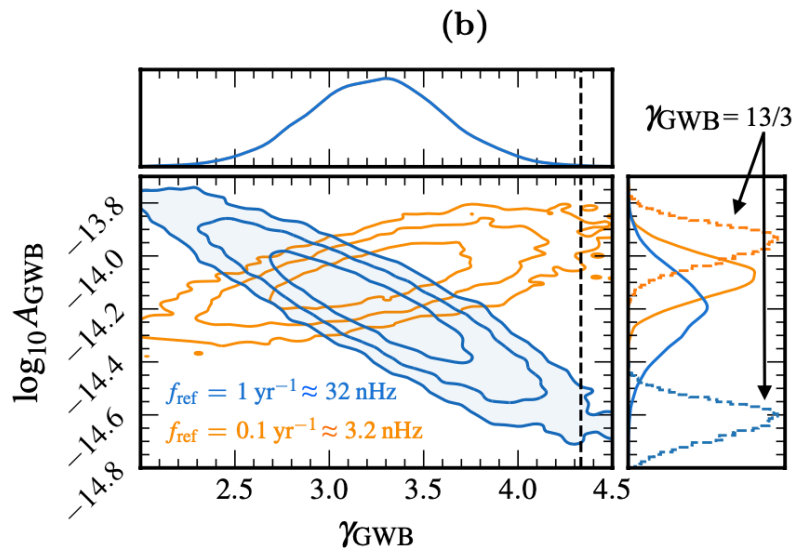
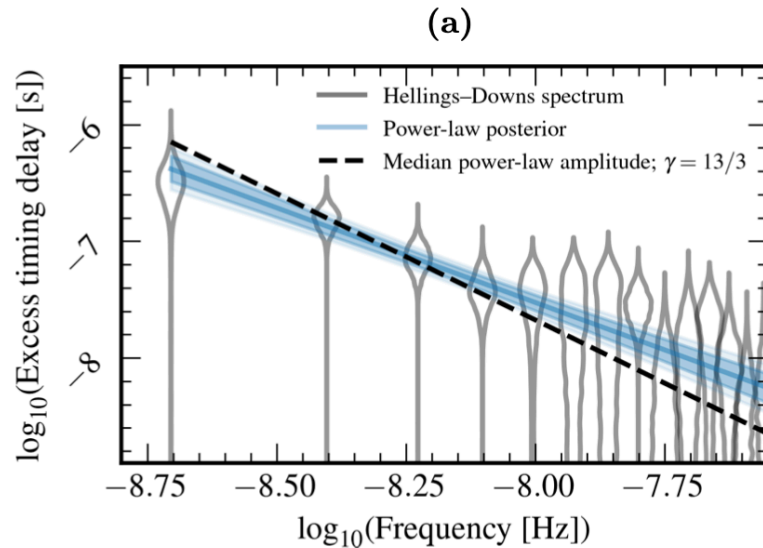
Detecting IMBH Mergers



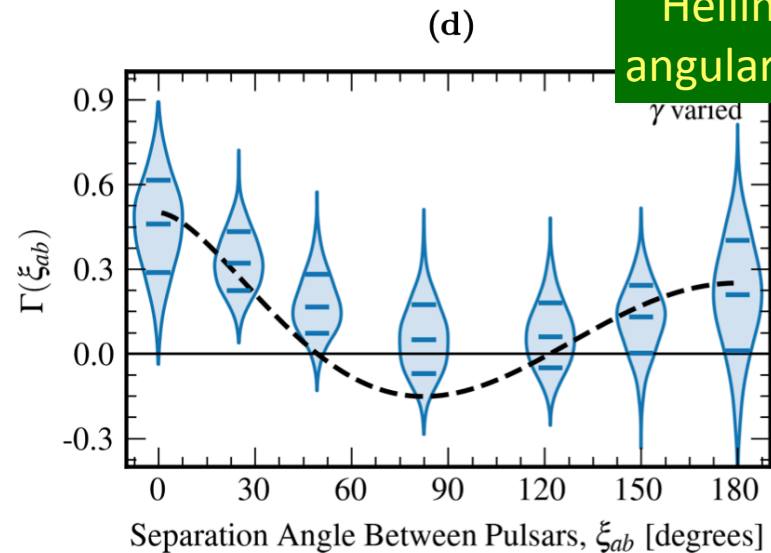
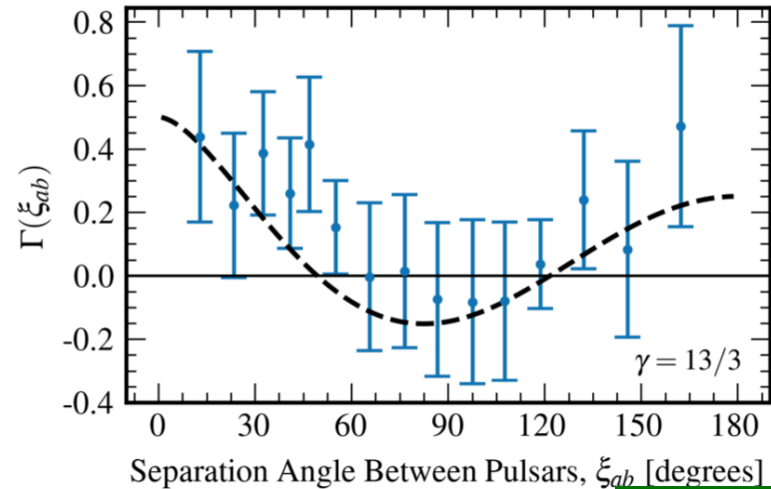
LISA and AEDGE would observe similar numbers of IMBH mergers
 AEDGE mergers would have been observed by LISA during infall
 Opportunities to test GR, multi-messenger astronomy

\mathcal{M}_0 = chirp mass, η = mass ratio

NANOGrav 15-Year Data



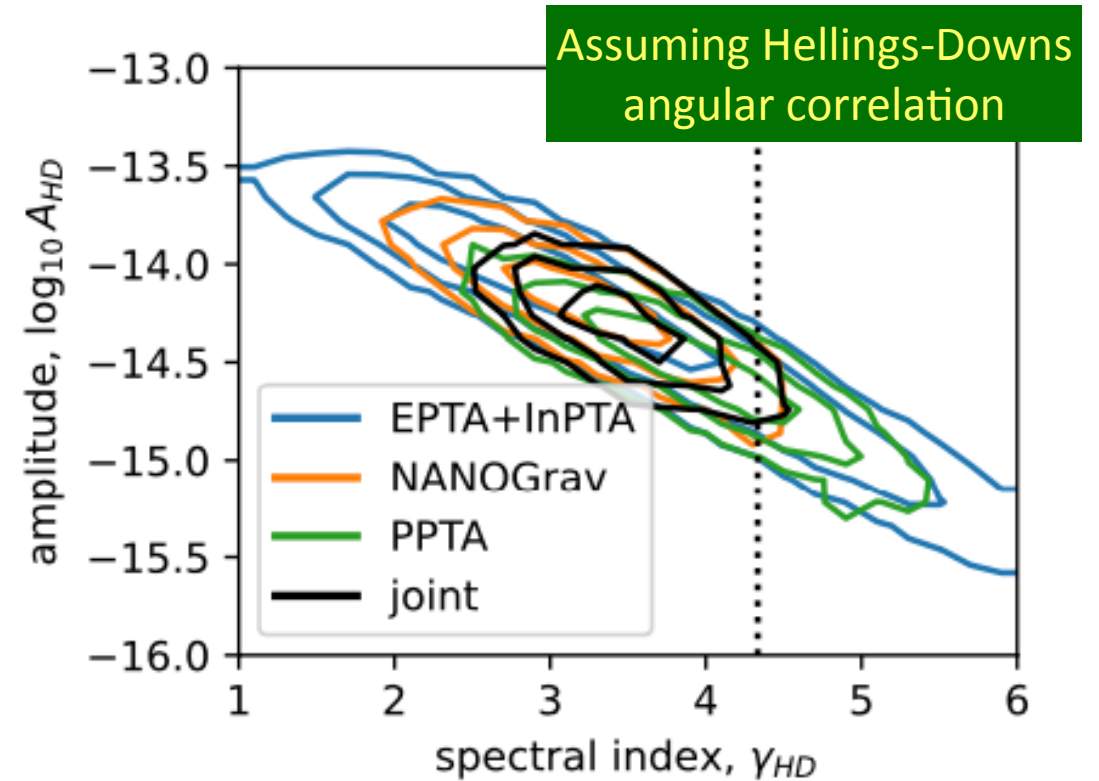
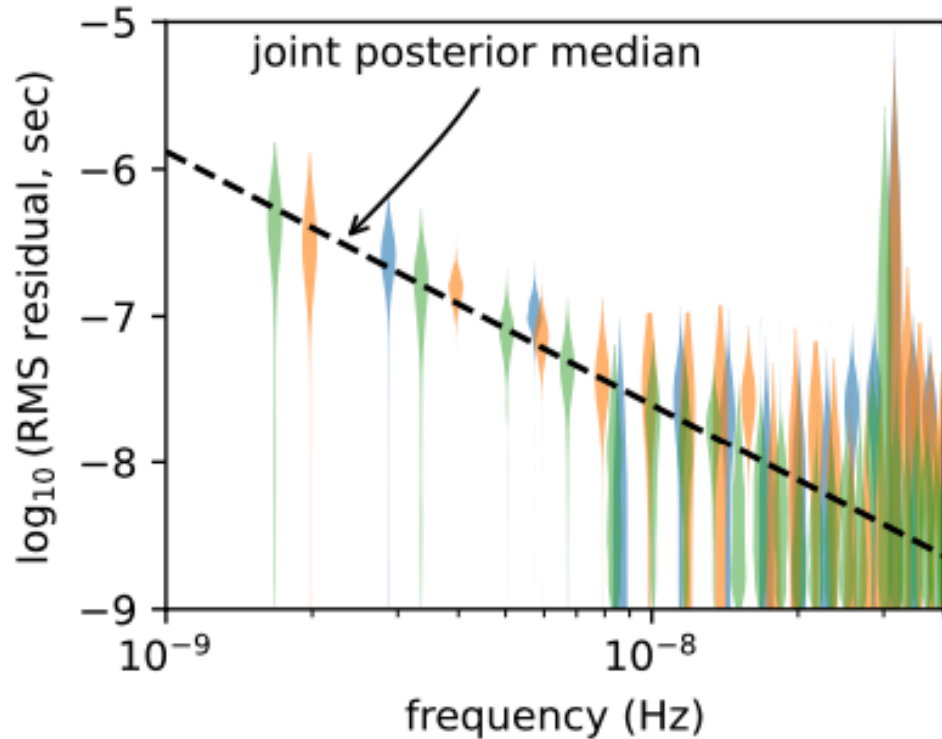
(c) NANOGrav GWs arXiv:2306.16213



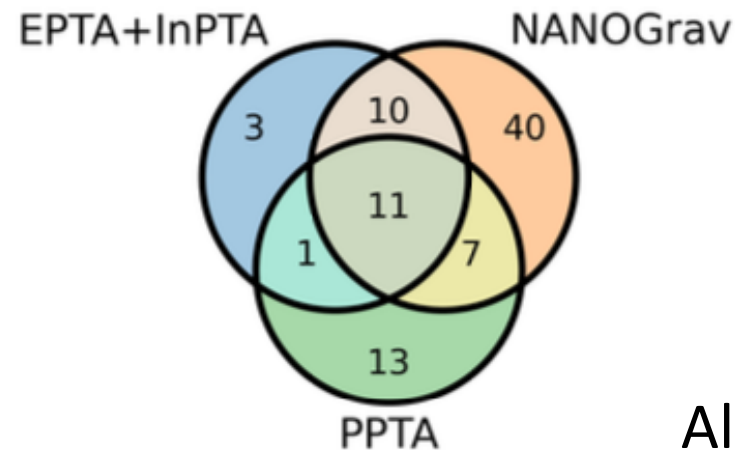
Hellings-Downs
angular correlation

Expect spectral index $\gamma = 13/3$ for SMBH binaries: not a good fit
 Evidence for GWs: Hellings-Downs angular correlation Bayes factor ~ 200

IPTA Data Compilation

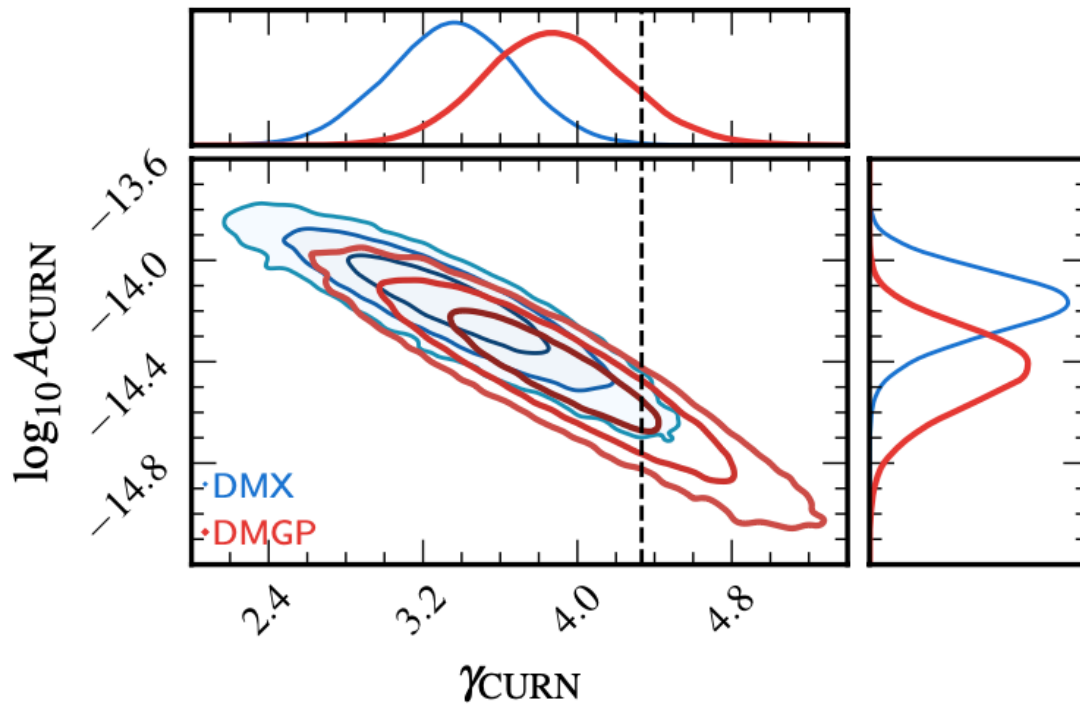


Venn diagram
of PTA data sets

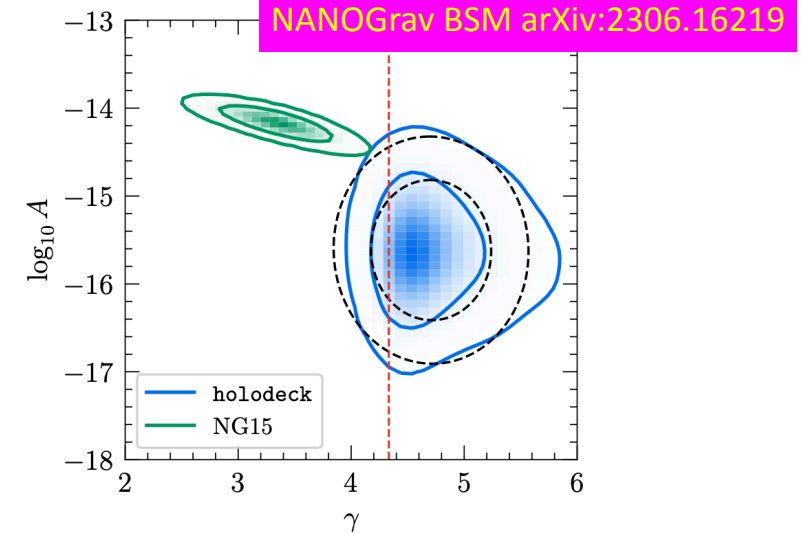


NANOGrav 15-Year Data

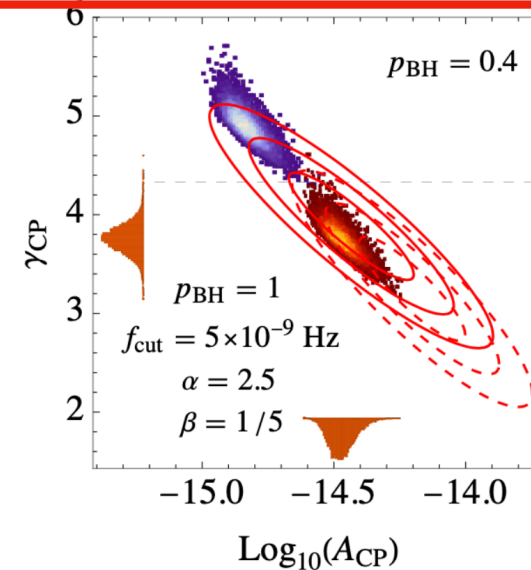
NANOGrav GWs arXiv:2306.16213



Range of γ depends on treatment of pulsar noise (spectrum not fitted well by single power law)



Prima facie disagreement with SMBH energy loss by GW alone



Consistent with environment + GWs

Environmental energy loss AION

- Interactions with gas, stars, dark matter?

- Total energy loss rate: $\dot{E} = -\dot{E}_{\text{GW}} - \dot{E}_{\text{env}}$

- Characteristic time scales: $t_{\text{GW}} \equiv E/\dot{E}_{\text{GW}} = 4\tau$, $t_{\text{env}} \equiv E/\dot{E}_{\text{env}}$

- Where $\tau = \frac{5}{256} (\pi f_r)^{-8/3} \mathcal{M}^{-5/3}$

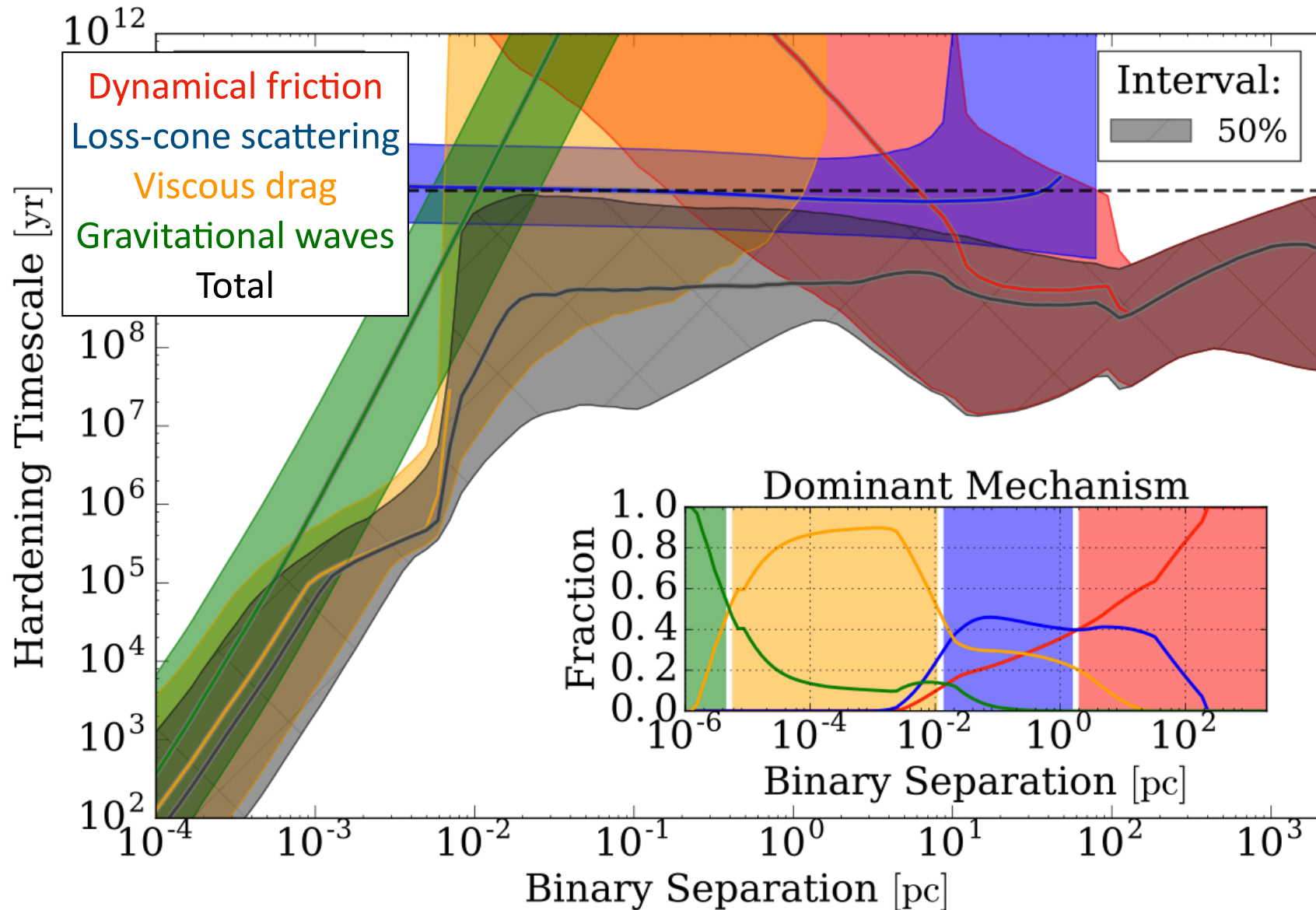
- Energy radiated in GWs reduced because of accelerated evolution:

$$\frac{dE_{\text{GW}}}{d \ln f_r} = \frac{1}{3} \frac{(\pi f_r)^{2/3} \mathcal{M}^{5/3}}{1 + t_{\text{GW}}/t_{\text{env}}}$$

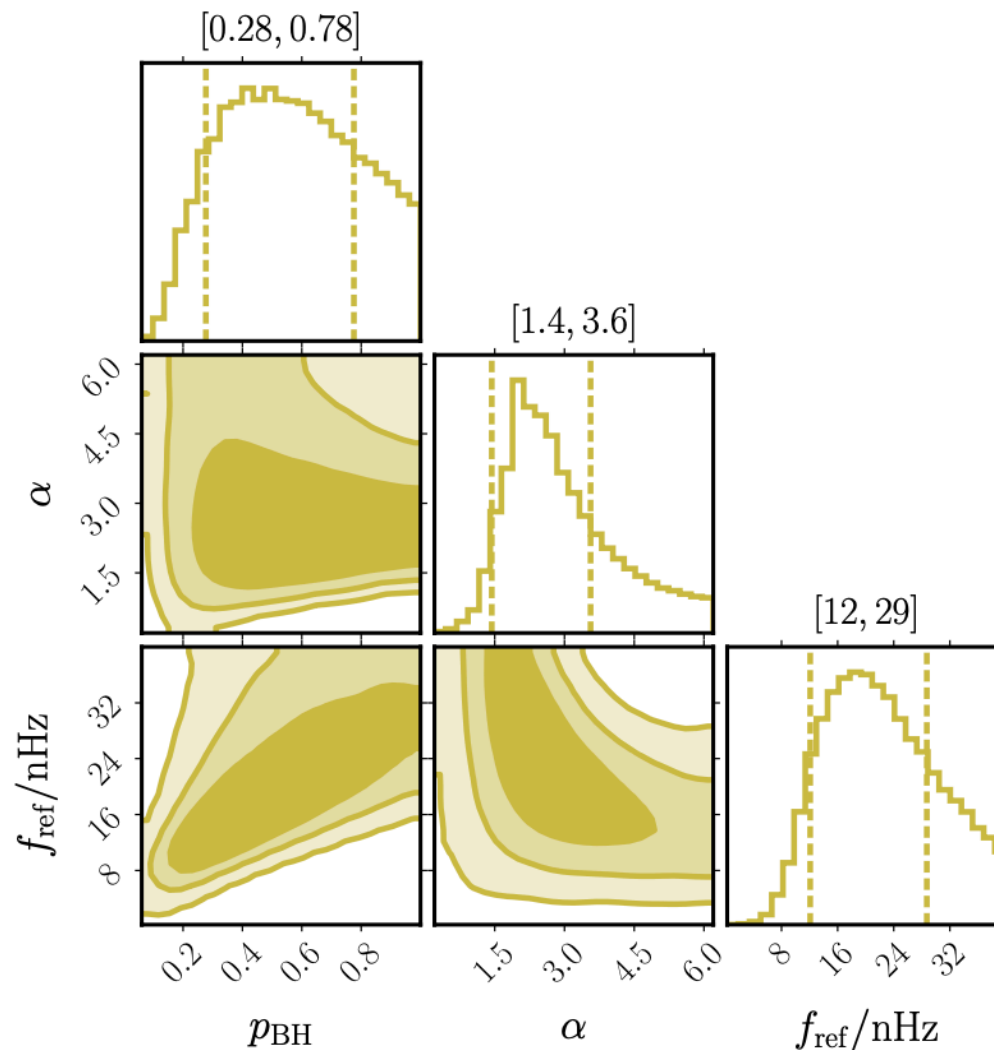
- Phenomenological parametrization:

$$\frac{t_{\text{env}}}{t_{\text{GW}}} = \left(\frac{f_r}{f_{\text{GW}}} \right)^\alpha, \quad f_{\text{GW}} = f_{\text{ref}} \left(\frac{\mathcal{M}}{10^9 M_{\text{sun}}} \right)^{-\beta}$$

Mechanisms for Energy Loss

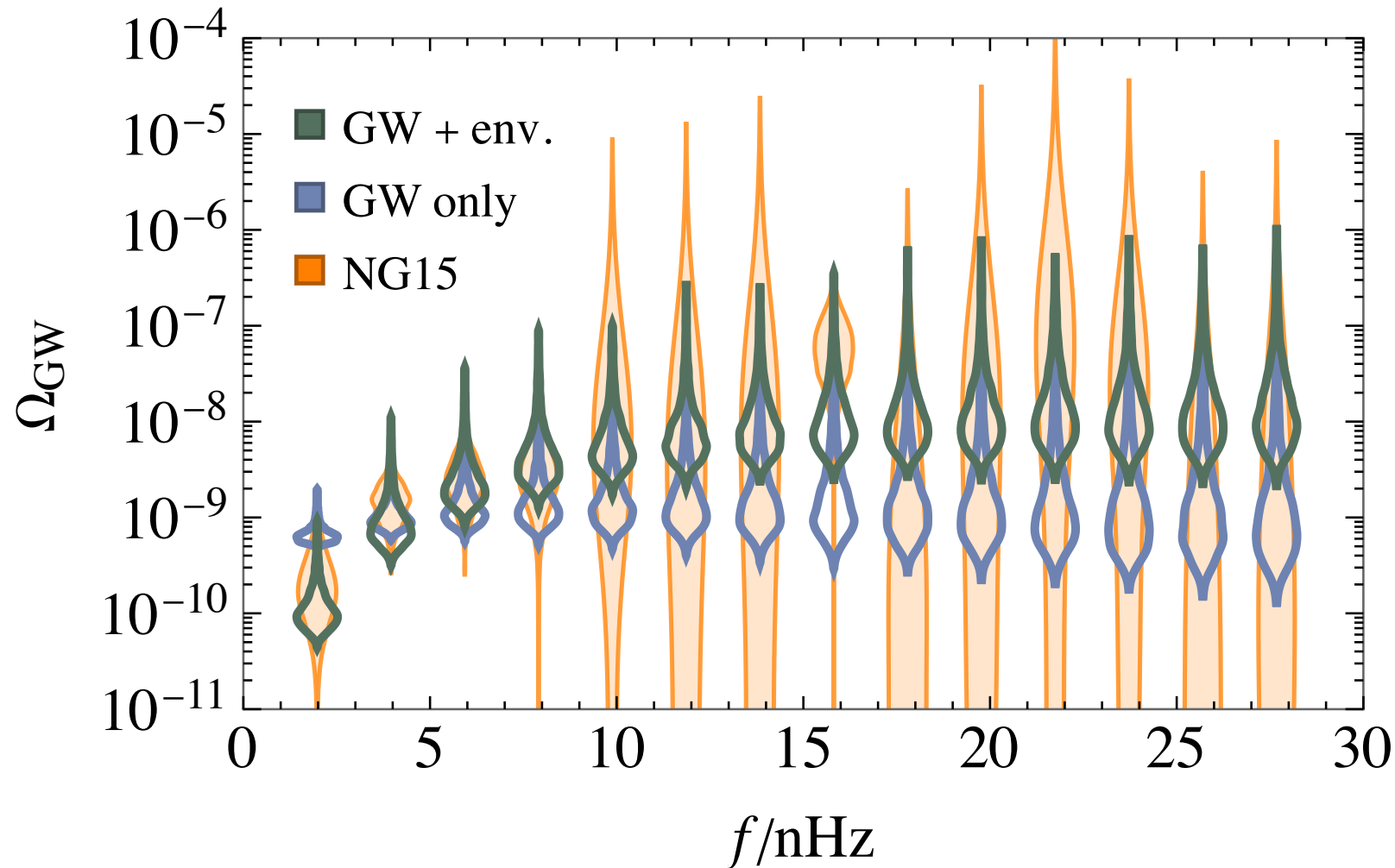


SMBH Fits to NANOGrav AION



SMBH binary model fits NANOGrav data better if environmental energy-loss effects are included

Astrophysical Interpretations

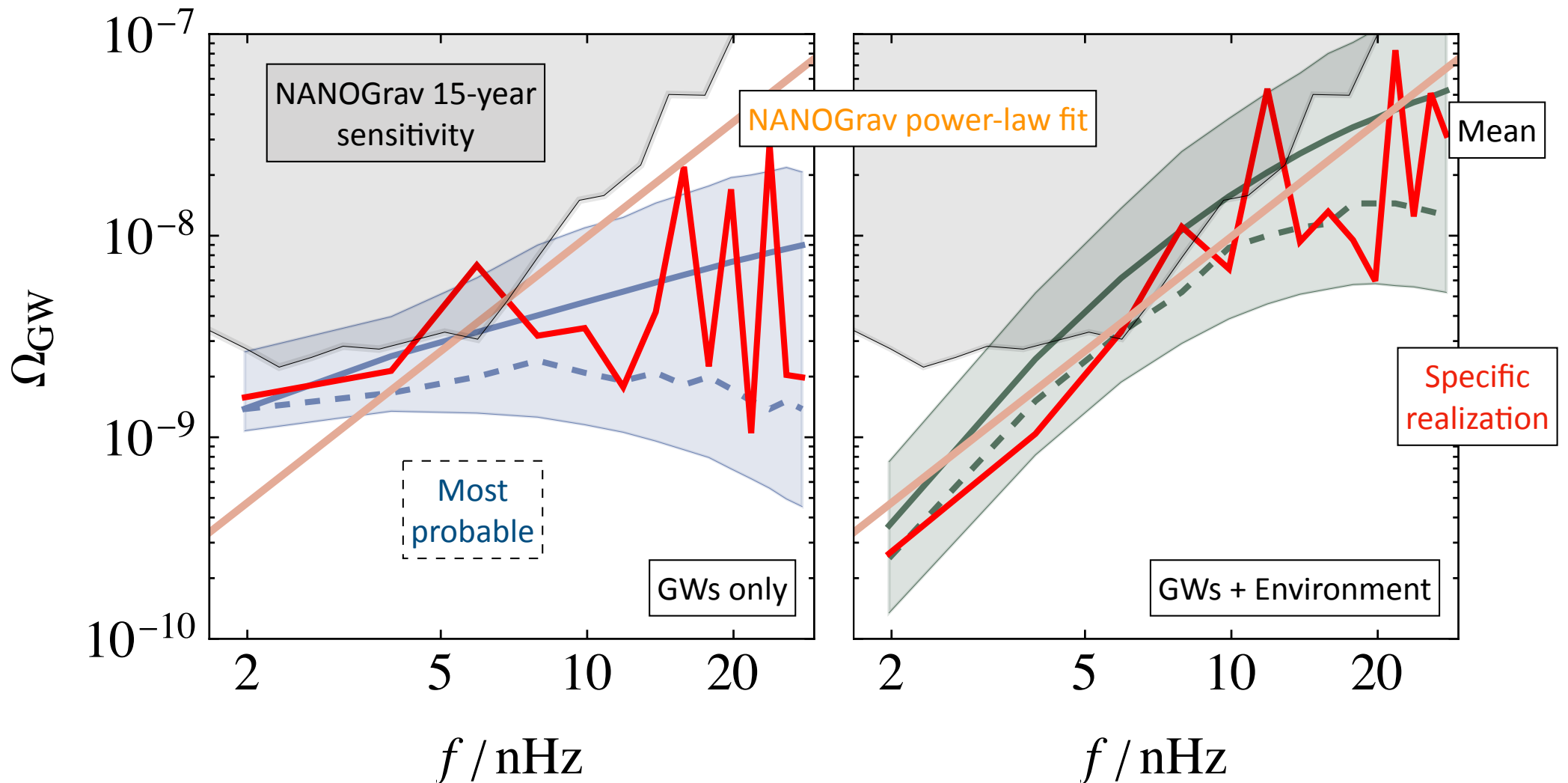


Fits use overlaps of data and model violins in each bin

NB: Fits go beyond simple power-law approximations

Better fit to spectrum if evolution driven by both environment & GWs

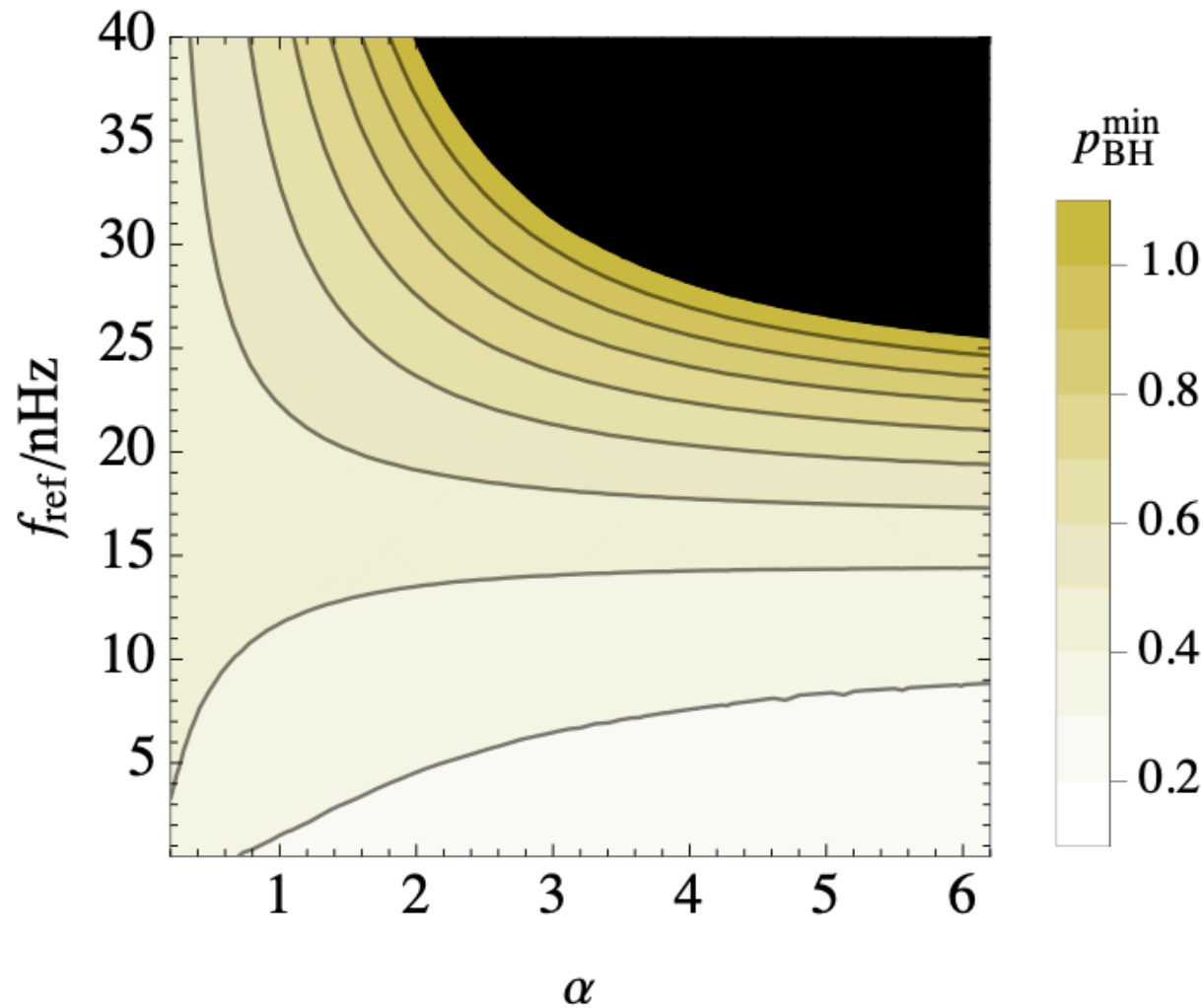
GWs + Environment? AION



Bigger chance to see specific binaries if evolution also driven by environment
(0.8 events vs 0.4 if GW only, most likely ~ 5 nHz)

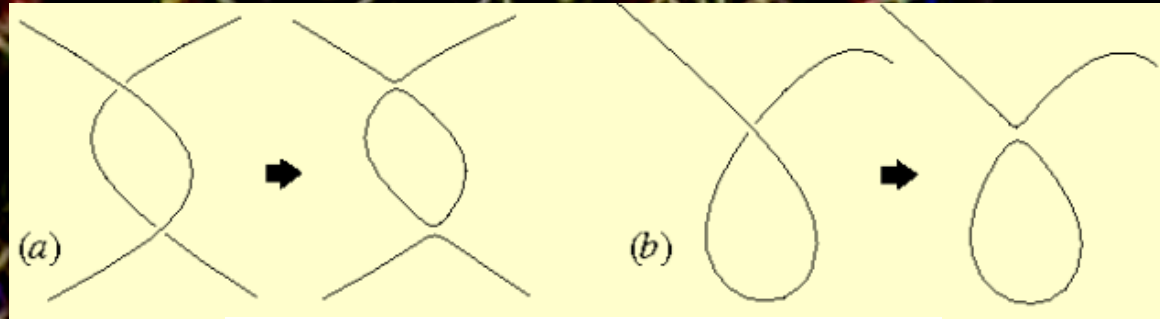
NANOGrav & EPTA @ 4 nHz? AION

NANOGrav and EPTA both report hint of up-fluctuation at ~ 4 nHz



Region of parameter space of SMBH + environment: probability $> 5\%$

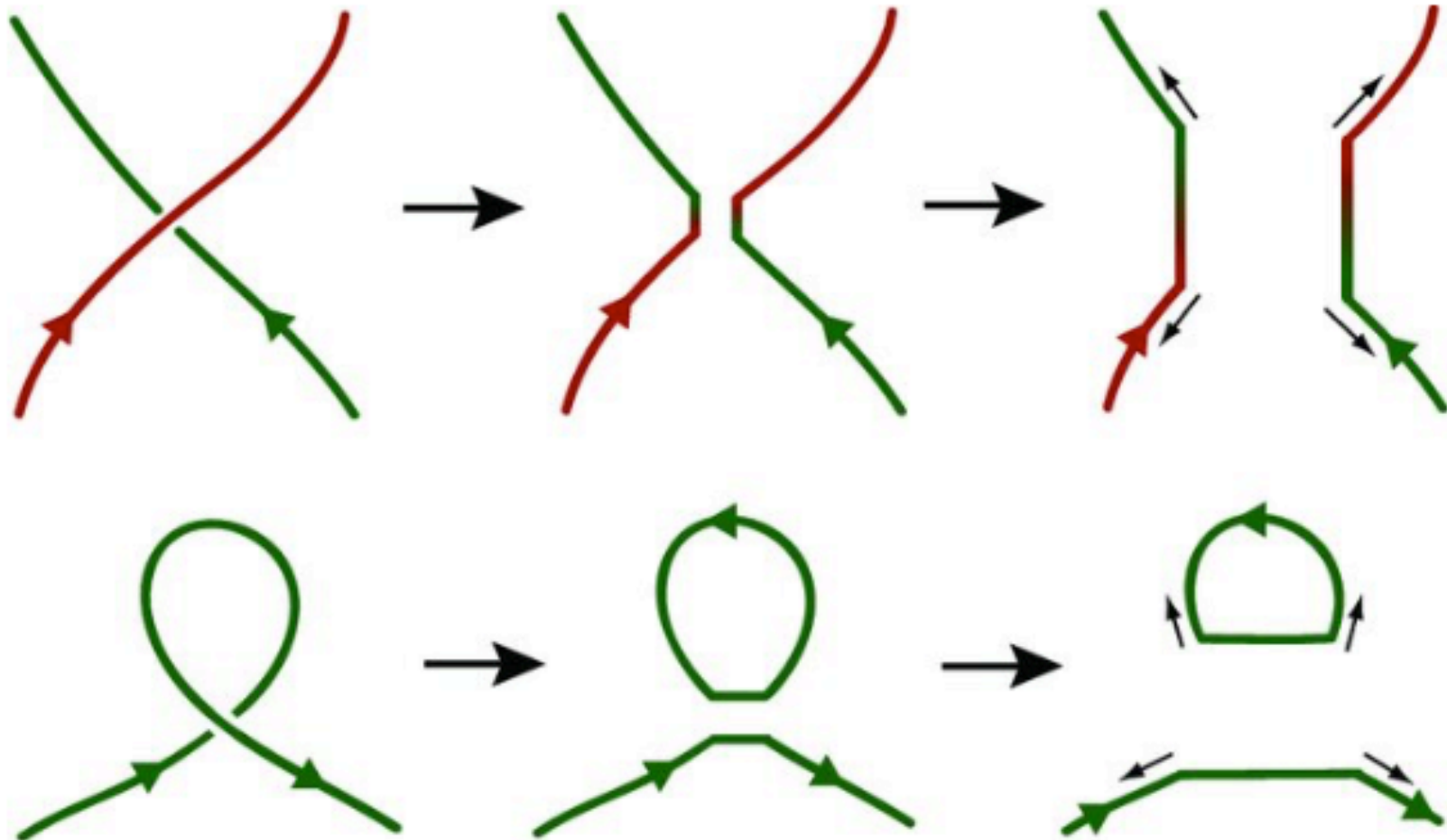
Probing Cosmic Strings



GW emission from string loops

Simulation of cosmic string network – Cambridge cosmology group

String Intercommutation



U(1) bosonic strings intercommute with probability $p = 1$
Other strings (super, QCD-like, ...) may have $p < 1$

Calculation of GWs from Cosmic Strings

- Use Velocity-dependent One-Scale (VOS) Model
- Network of strings produces loops, lengths:

$$\ell = \alpha_\ell t_i - \Gamma G\mu(t - t_i)$$

- Loops emit at normal mode frequencies:

$$f = \frac{a(\tilde{t})}{a(t_0)} \frac{2k}{\alpha_\ell t_i - \Gamma G\mu(\tilde{t} - t_i)}$$

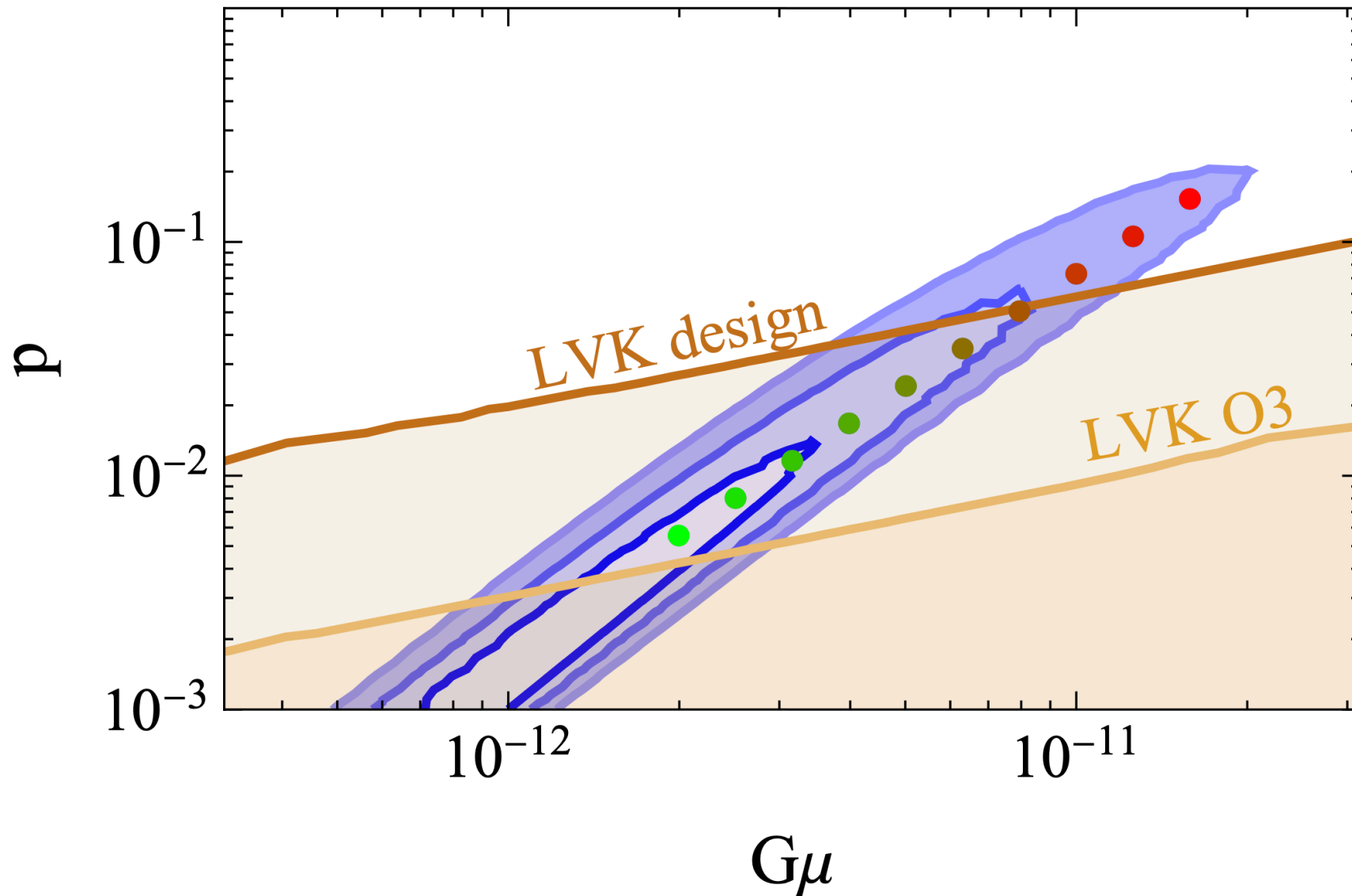
- Density of GWs: $\Omega_{GW}^{CS}(f) = \sum_{k=1}^{\infty} k \Gamma^{(k)} \Omega_{GW}^{(k)}(f)$, $\Gamma^{(k)} = \Gamma k^{-\frac{4}{3}} / (\sum_{m=1}^{\infty} m^{-\frac{4}{3}})$

$$\Omega_{GW}^{(k)}(f) = \frac{16\pi}{3H_0^2} \frac{(0.1)(G\mu)^2}{\alpha_\ell(\alpha_\ell + \Gamma G\mu)} \frac{1}{f} \times \int_{t_F}^{t_0} d\tilde{t} \frac{C_{eff}(t_i)}{t_i^4} \left(\frac{a(\tilde{t})}{a(t_0)}\right)^5 \left(\frac{a(t_i)}{a(\tilde{t})}\right)^3 \Theta(t_i - t_F)$$

where factor 0.1, $\Gamma \simeq 50$ from simulations,

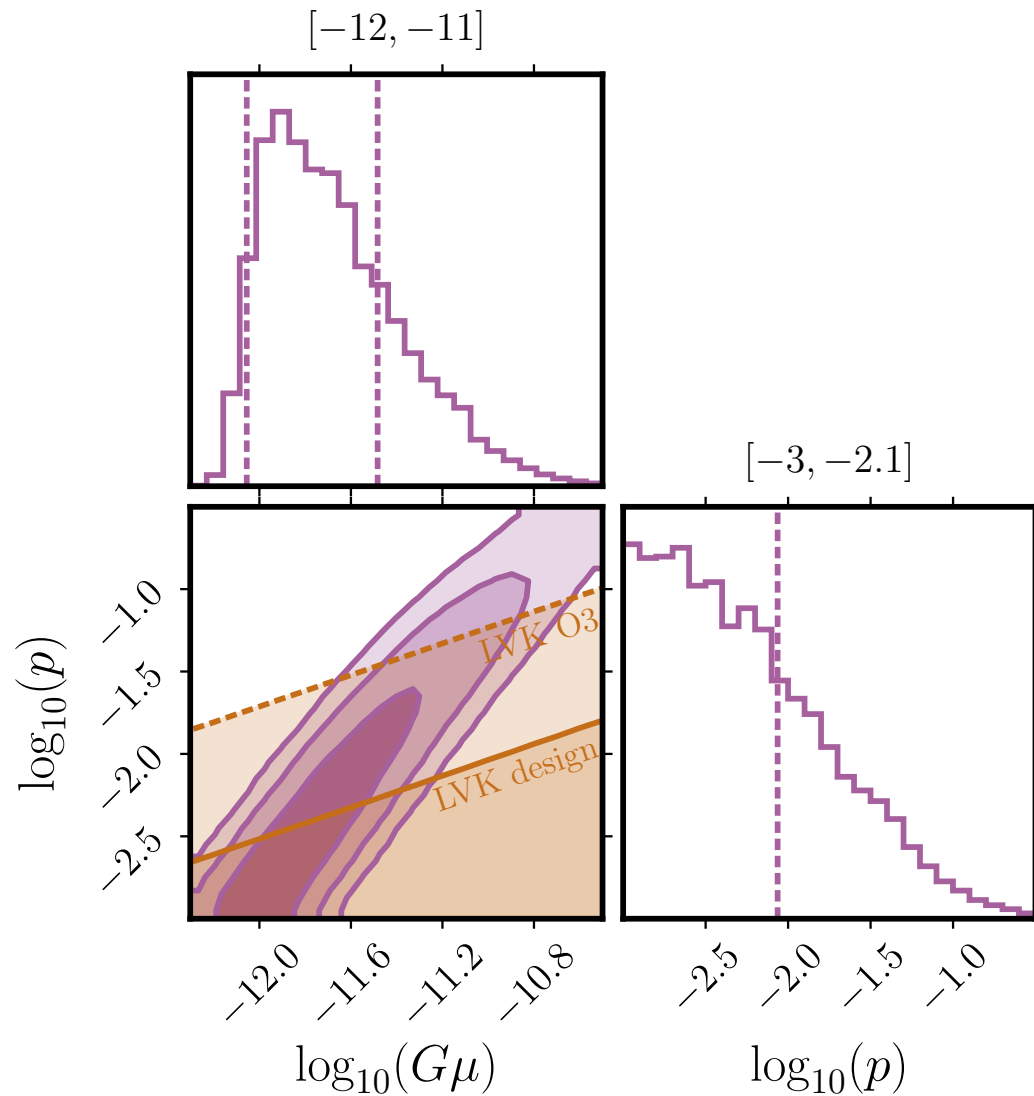
$C_{eff} = 5.4$ (0.39) during radiation (matter) domination

Superstrings vs LVK



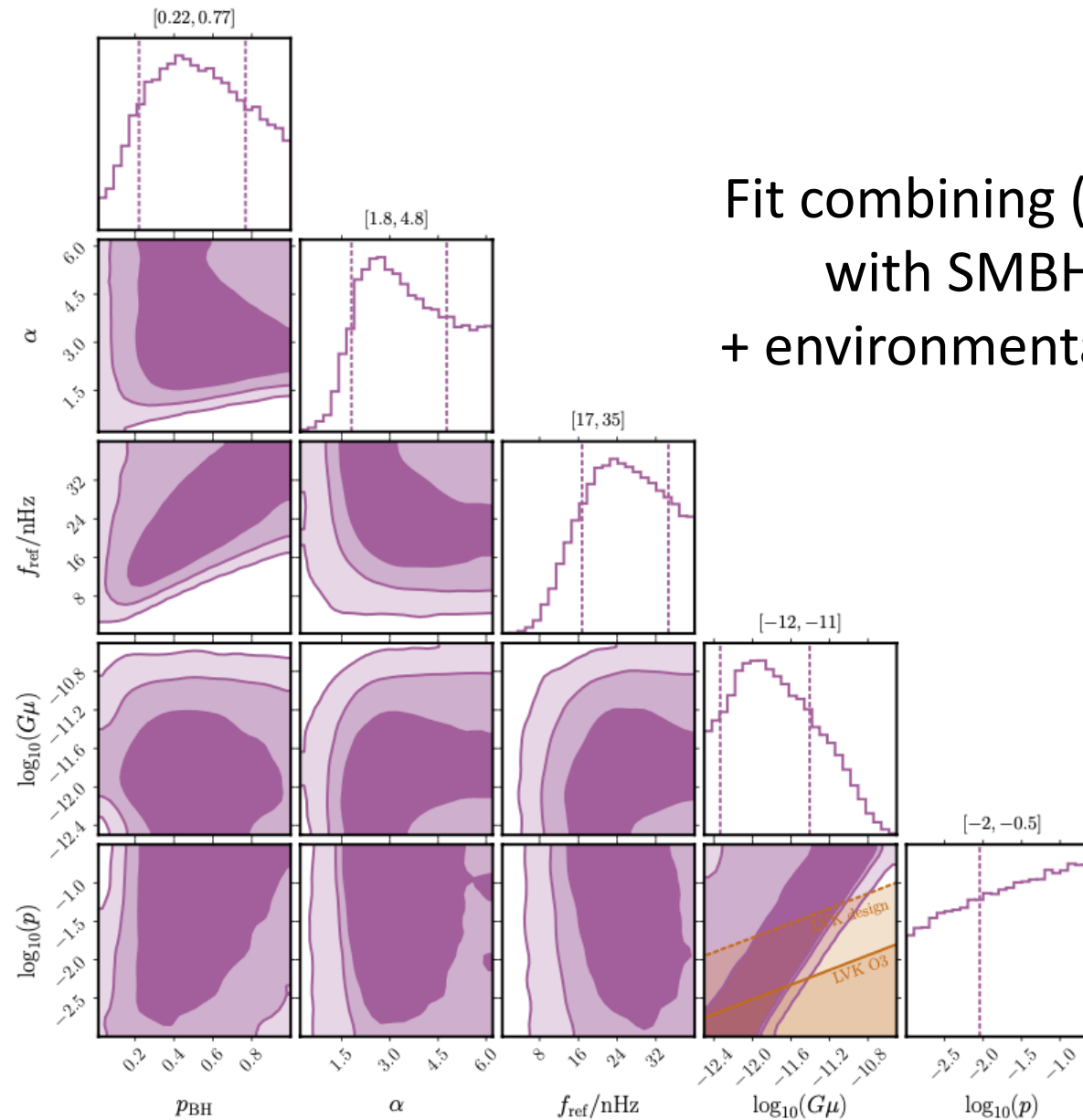
(Super)string model compatible with LVK for $p \sim 0.001 - 0.1$

Superstring Fit to NANOGrav



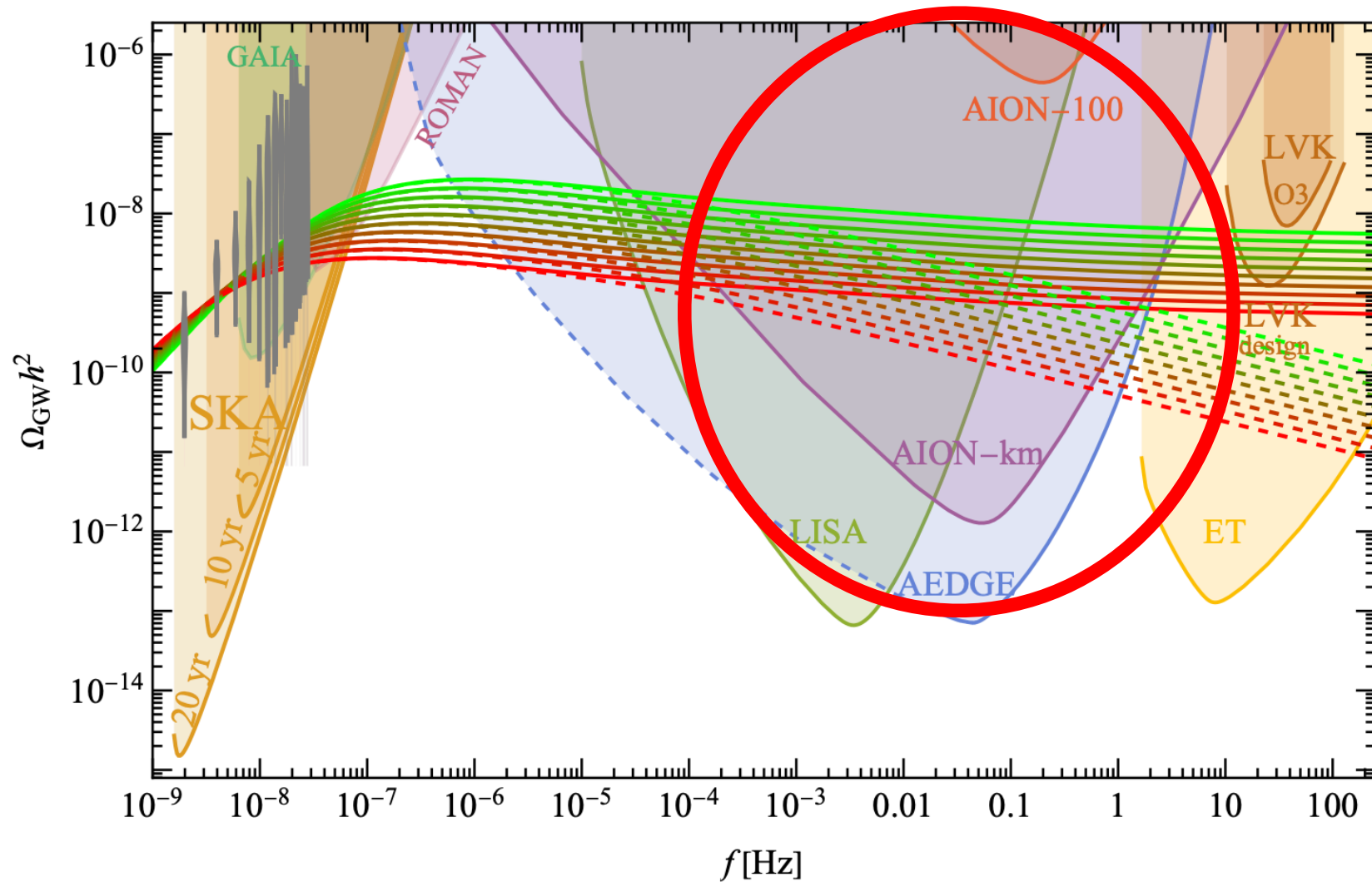
(Super)string model compatible with LVK for string tension $G\mu \sim 10^{-12} - 10^{-11}$,
intercommutation probability $p \sim 0.001 - 0.01$

Superstring + SMBH Fit



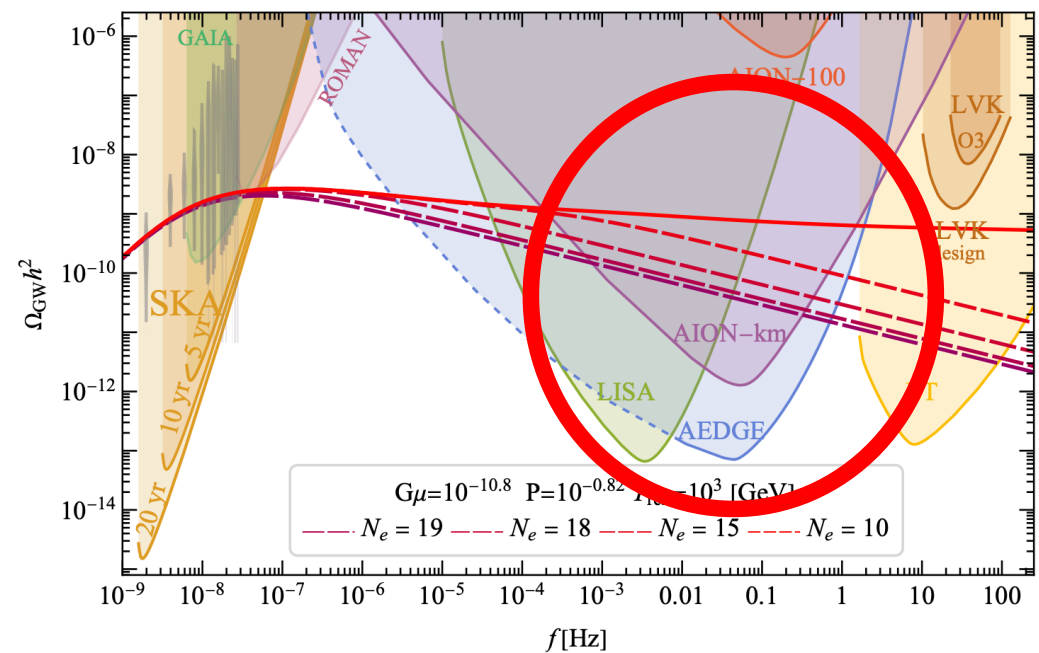
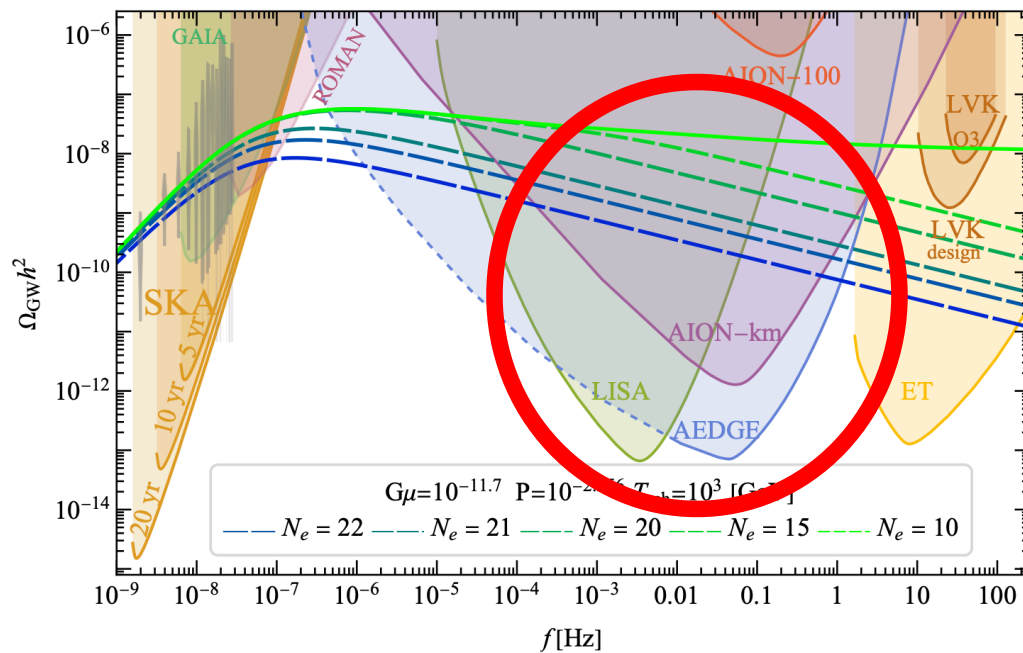
Fit combining (super)strings
with SMBH binaries
+ environmental energy loss

Effect of Matter Domination



Late period of matter domination could push superstrings beyond LVK, but still detectable by LISA, AION/AEDGE, ET

Effects of Thermal Inflation



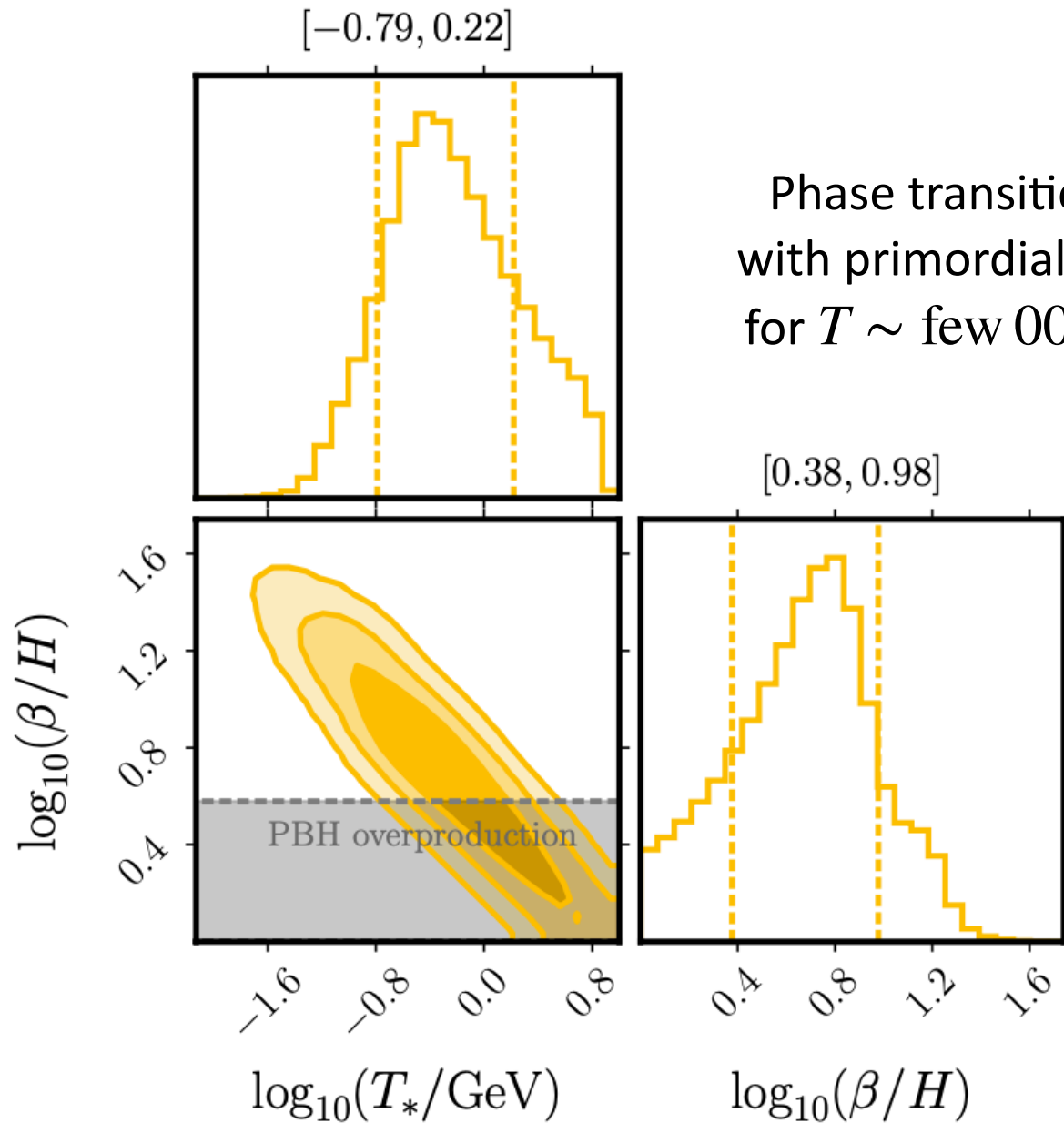
Could also push superstrings beyond LVK,
but still detectable by LISA, AION/AEDGE, ET

Probing Cosmological Phase Transitions

The background of the slide is a complex, colorful simulation of bubble collisions. It features a network of interconnected, glowing structures in shades of orange, yellow, green, and blue against a dark background. These structures resemble a web of filaments and loops, characteristic of topological defects or phase transition remnants in cosmology.

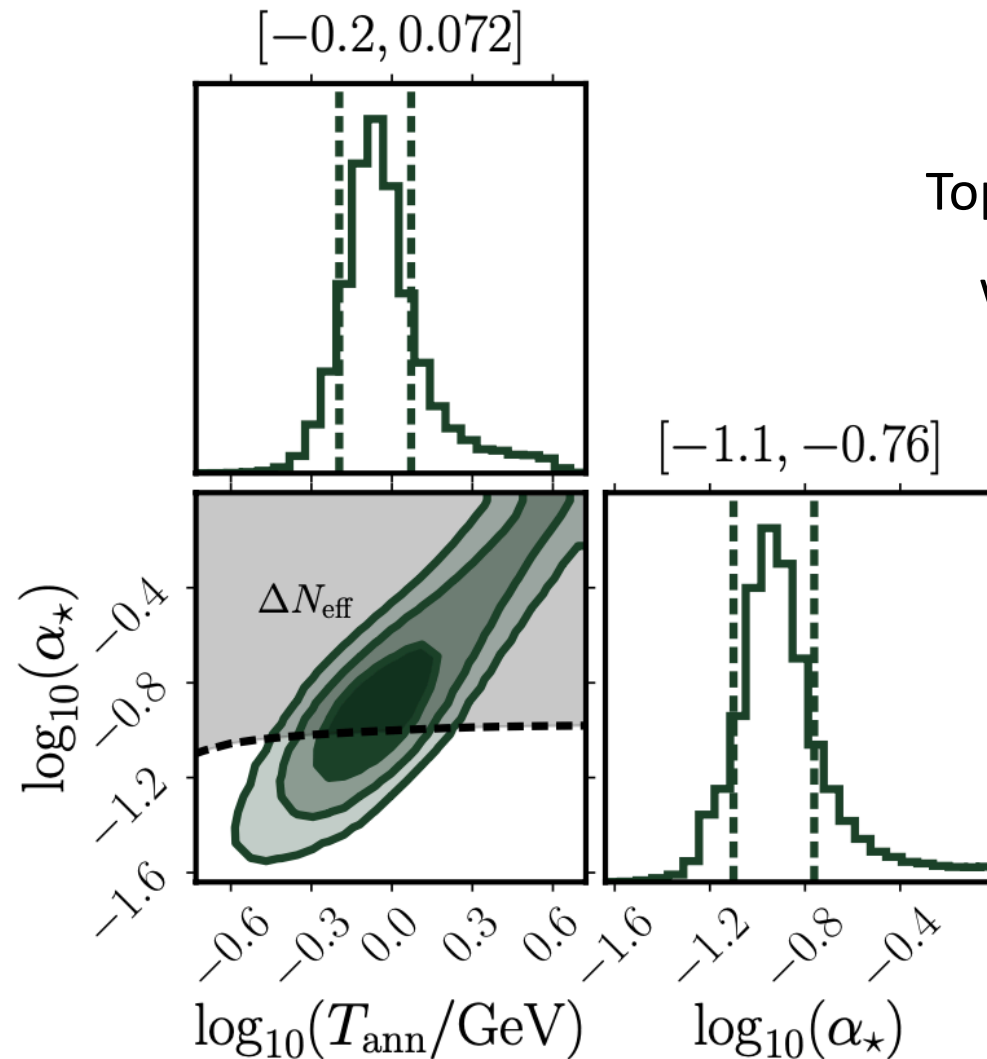
Simulation of bubble collisions – D. Weir

Phase Transition Fit to NANOGrav AION



Phase transition model compatible with primordial black hole abundance for $T \sim \text{few } 00 \text{ MeV}$ (hidden sector)

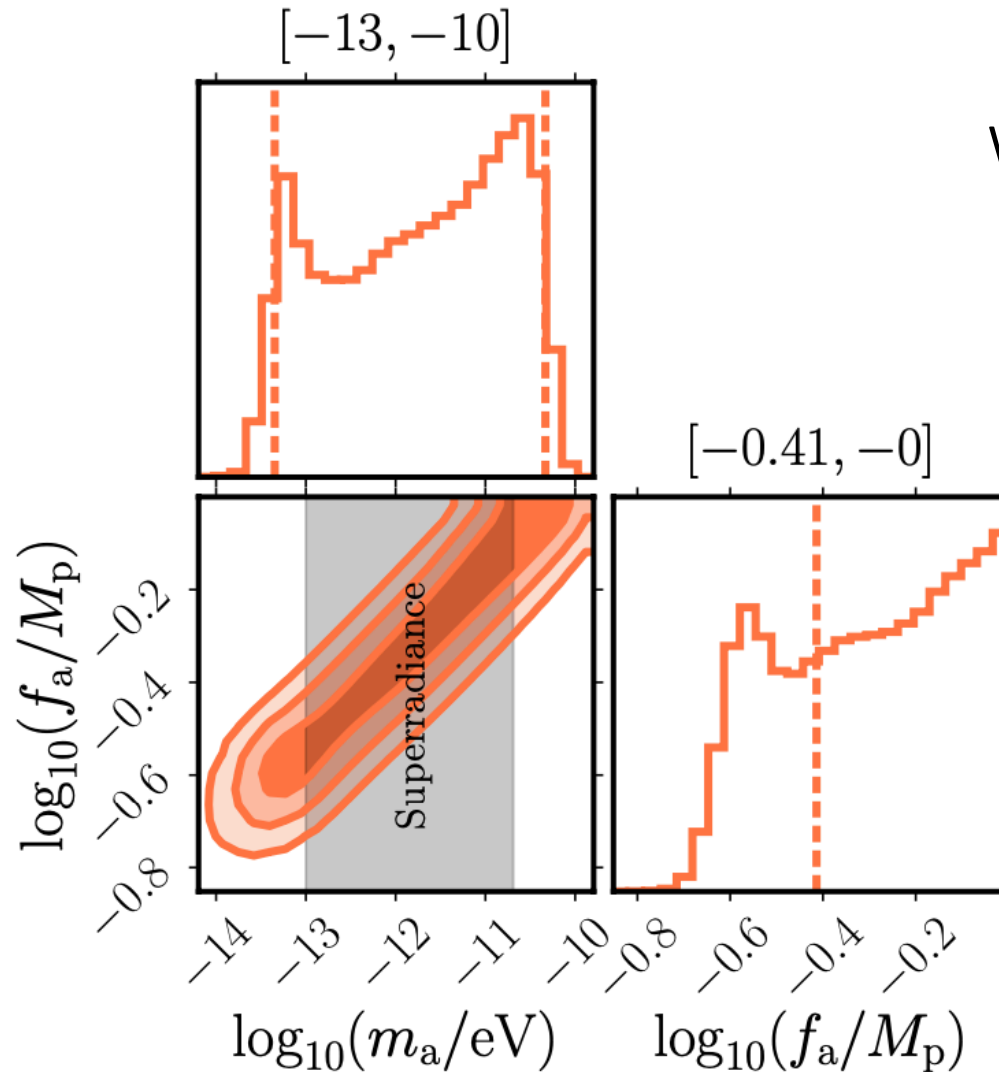
Domain Wall Fit to NANOGrav AION



Topological defects produced when discrete symmetry is broken after inflation

Domain wall model compatible with cosmology for annihilation temperature $T_{\text{ann}} \sim \text{GeV}$ (hidden sector)

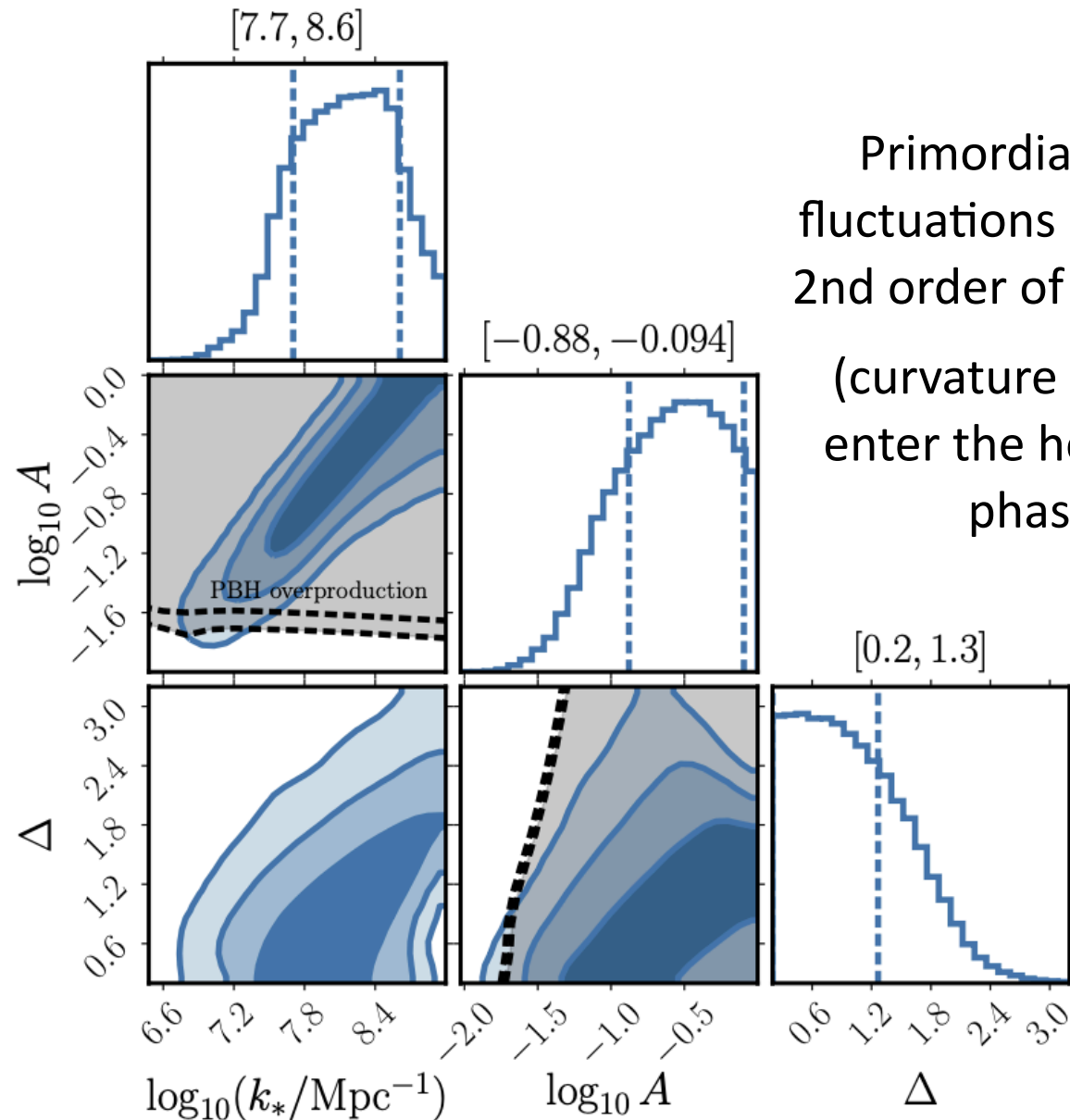
Axion Fit to NANOGrav AION



When an axion-like particle has weak coupling to SM, GWs can be produced via tachyonic instability
light dark photon helicity state

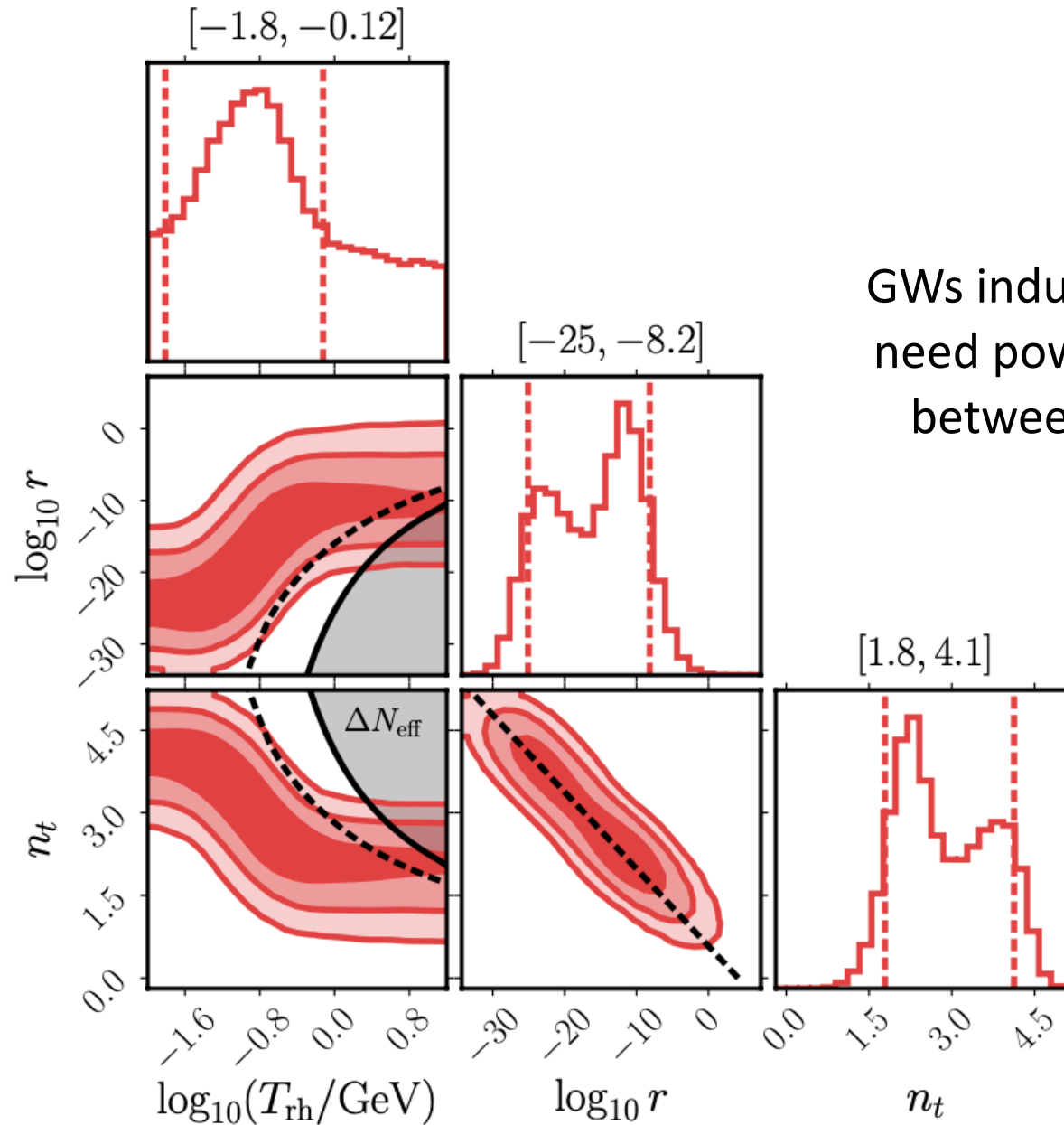
Axion model compatible with cosmology for $m_a \sim 10^{-13}$ or $\sim 10^{-10}$ eV, $f_a \sim 10^{-6}$ or $\sim \mathcal{O}(1) M_P$

Scalar-Induced GWs Fit to NANOGrav



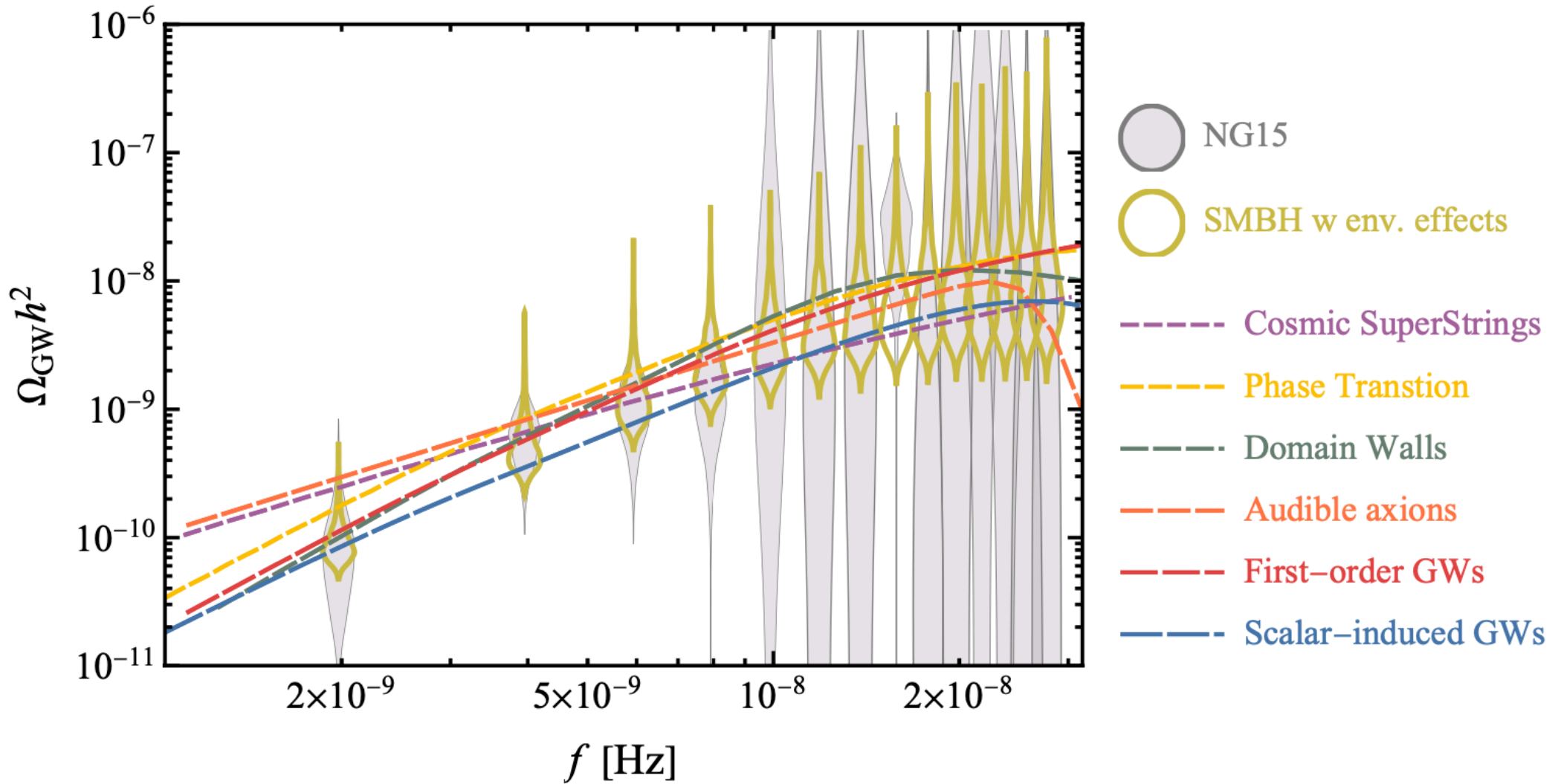
Primordial scalar curvature fluctuations can produce GWs at 2nd order of perturbation theory (curvature perturbations that enter the horizon around QCD phase transition)

First-Order GWs Fit to NANOGrav

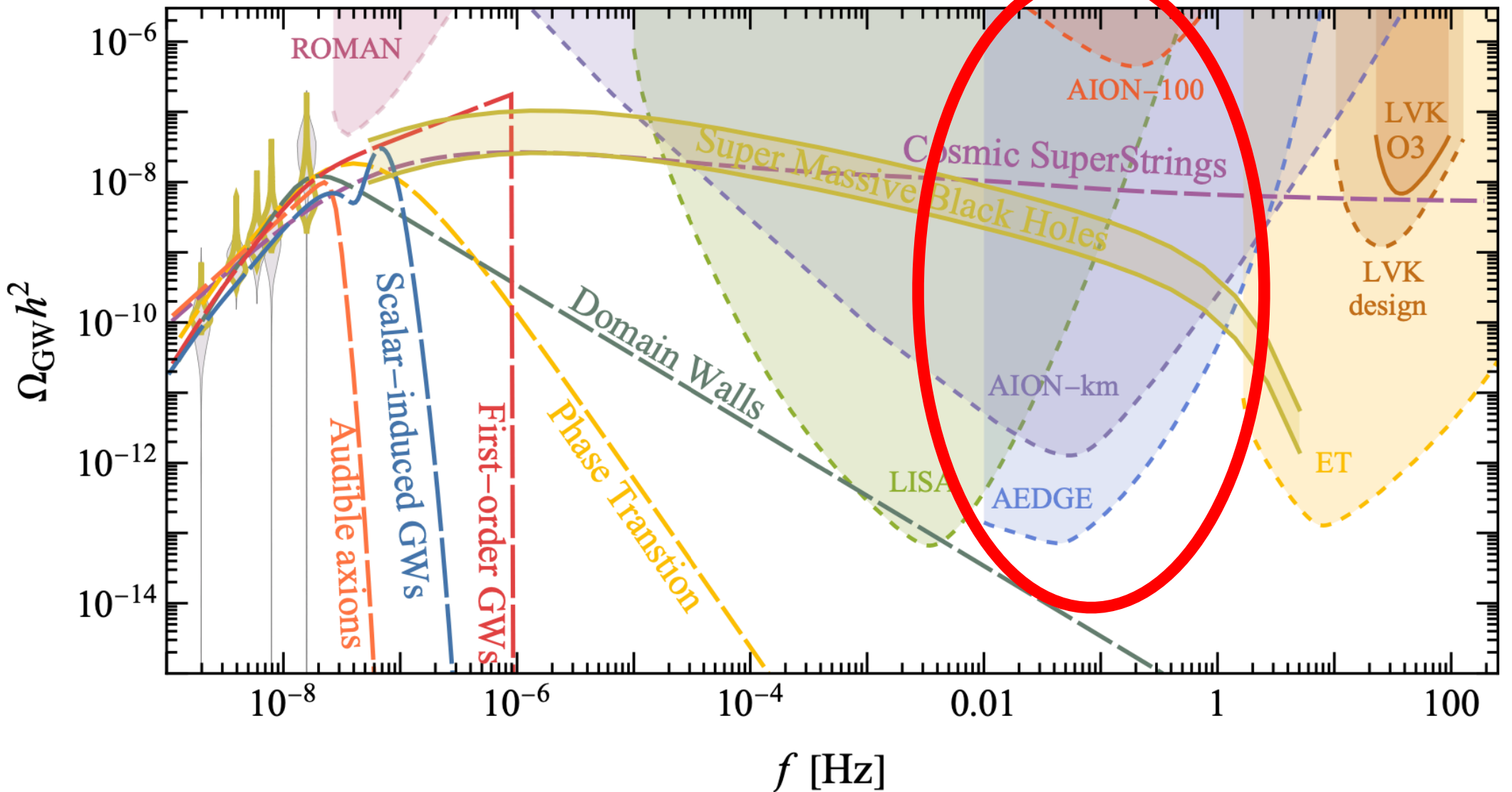


GWs induced at first order:
 need power-law spectrum
 between CMB and PTA
 scales

Fits to NANOGrav



Extension of Fits to Higher Frequencies



Results For NANOGrav Fits

Results from Multi-Model Analysis (MMA)

Scenario	Best-fit parameters	ΔBIC	Signatures
GW-driven SMBH binaries	$p_{\text{BH}} = 0.07$	6.0	FAPS, LISA, mid- f , LVK, ET
GW + environment-driven SMBH binaries	$p_{\text{BH}} = 0.84$ $\alpha = 2.0$ $f_{\text{ref}} = 34 \text{ nHz}$	Baseline (BIC = 53.9)	FAPS, LISA, mid- f , LVK, ET
Cosmic (super)strings (CS)	$G\mu = 2 \times 10^{-12}$ $p = 6.3 \times 10^{-3}$	-1.2 (4.6)	FAPS, LISA, mid-f, LVK, ET
Phase transition (PT)	$T_* = 0.34 \text{ GeV}$ $\beta/H = 6.0$	-4.9 (2.9)	FAPS, LISA, mid-f, LVK, ET
Domain walls (DWs)	$T_{\text{ann}} = 0.85 \text{ GeV}$ $\alpha_* = 0.11$	-5.7 (2.2)	FAPS, LISA?, mid-f, LVK, ET
Scalar-induced GWs (SIGWs)	$k_* = 10^{7.7}/\text{Mpc}$ $A = 0.06$ $\Delta = 0.21$	-2.1 (5.8)	FAPS, LISA, mid-f, LVK, ET
First-order GWs (FOGWs)	$\log_{10} r = -14$ $n_t = 2.6$ $T_{\text{rh}} = -0.67 \text{ GeV}$	-2.0 (6.0)	FAPS, LISA, mid-f, LVK, ET
“Audible” axions	$m_a = 3.1 \times 10^{-11} \text{ eV}$ $f_a = 0.87 M_{\text{P}}$	-4.2 (3.7)	FAPS, LISA, mid-f, LVK, ET

FAPS \equiv fluctuations, anisotropies, polarization, sources, mid- f \equiv mid-frequency experiment, e.g., AION [308], AEDGE [310], LVK \equiv LIGO/Virgo/KAGRA [161–163], ET \equiv Einstein Telescope [312] (or Cosmic Explorer [313]), signature \equiv not detectable

Quo Vadis NANOGrav?

- **Astrophysics or fundamental physics?**
- Biggest bangs since the Big Bang, or physics beyond the SM?
- SMBH binaries driven by GWs alone disfavoured
- SMBH binaries driven by GWs and environmental effects fit better
- **Better fits with cosmological BSM models**
- Discrimination possible with future measurements: fluctuations, anisotropies, polarization, experiments at higher frequencies - including atom interferometers
- **Time and more data will tell!**

