

Gravitational Wave Constraints on Properties of Exotic Compact Objects



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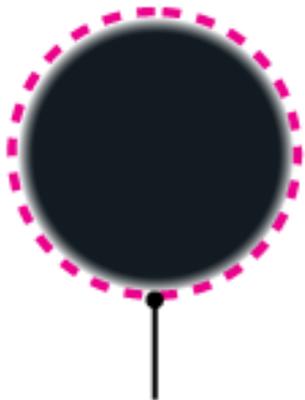


Exotic compact objects (ECOs)

Alternatives to BH in GR

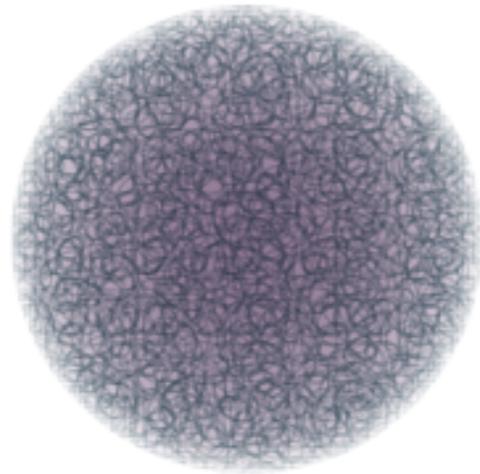
Motivation: avoid spacetime singularity in BH, and solve information loss problem of BH.

“Classical” black hole

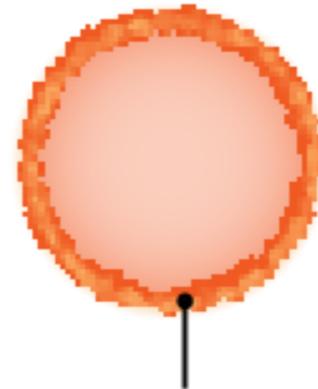


Event horizon

Fuzzball

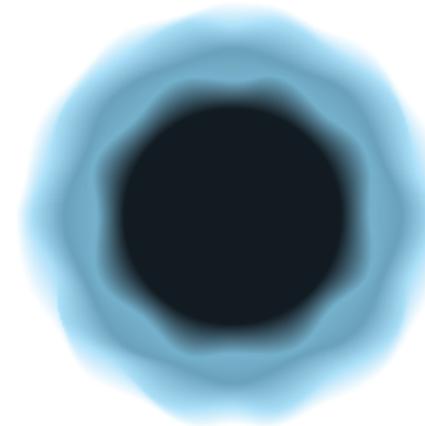


Firewall

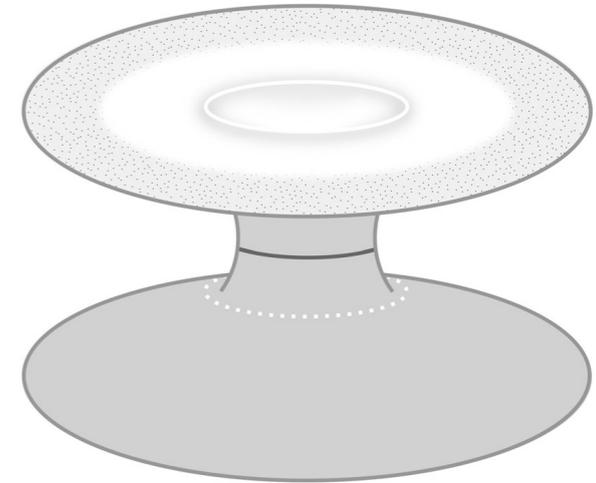


Wall of particles

Quantum halo

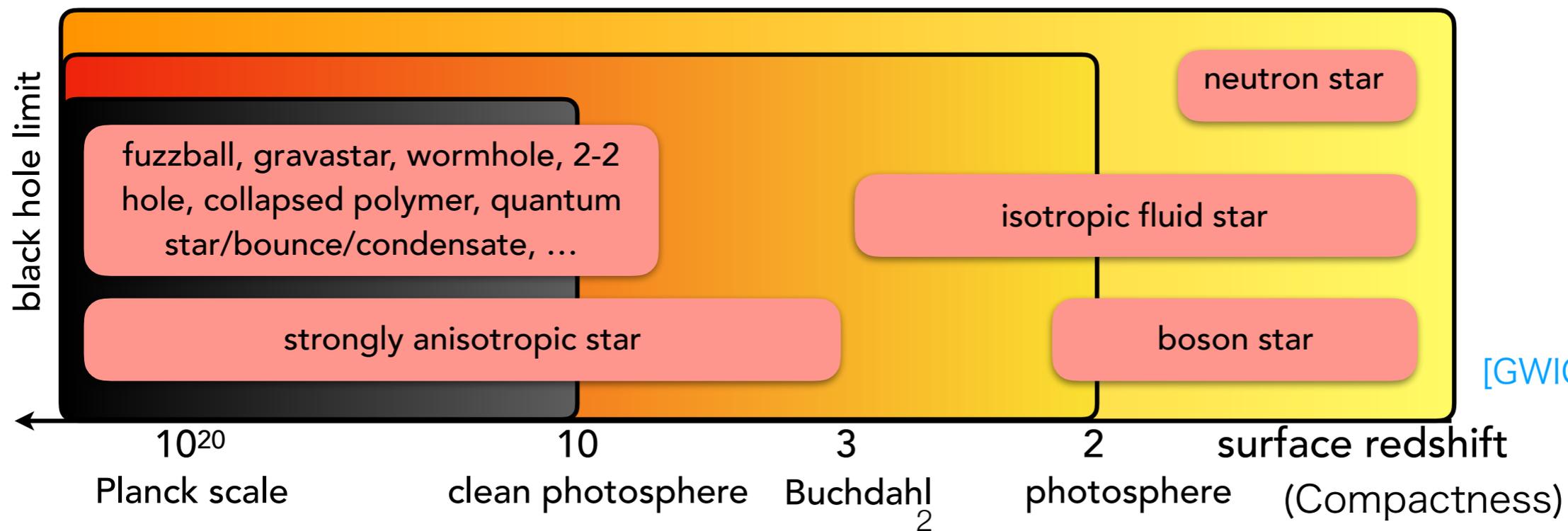


Wormhole



[Credit: Amanda Montanez, Scientific American, 2019]

[Cardoso, Pani, 2019]



[GWIC-3G science-case]

Properties of ECOs

Tidal deformability



Spin-Induced Quadrupole Moment
(SIQM)



ECOs have largely different values of Λ and $\delta\kappa$ from those of BHs.

Previous works: focusing on only one of Λ and $\delta\kappa$

Aim of this work:

Focusing on both Λ and $\delta\kappa$.

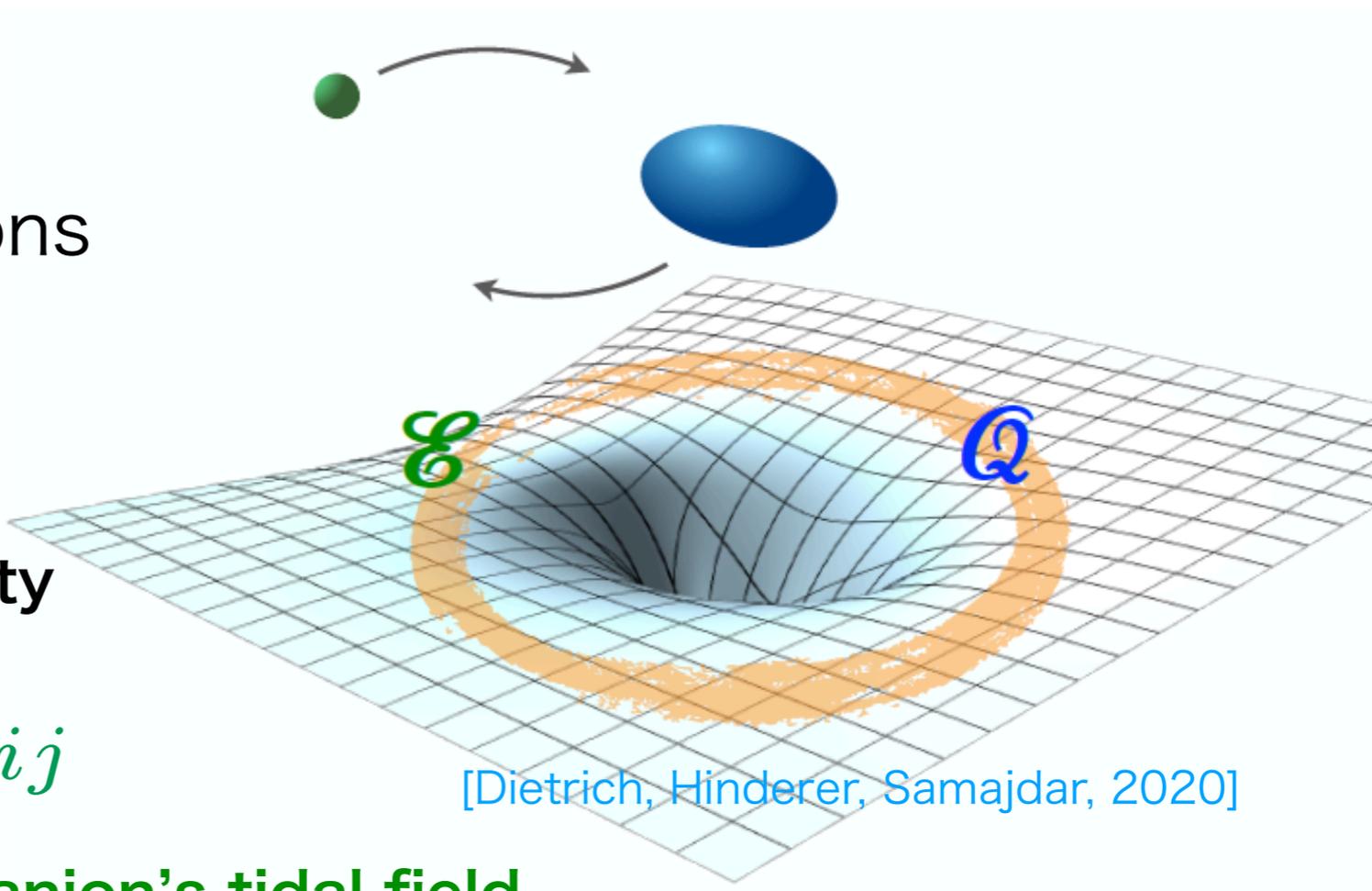
Model-independent constraints on deviations from the BBH case by measuring Λ and $\delta\kappa$ via GWs.



We report constraints on Λ and $\delta\kappa$ for six low-mass GWTC-2 events (long-inspiral regime): GW151226, GW170608, GW190707, GW190720, GW190728, GW190924

Tidal deformability

When binary orbital separations are small, each star is tidally distorted by its companion.



Tidal deformability

$$Q_{ij} = -\lambda \mathcal{E}_{ij}$$

[Dietrich, Hinderer, Samajdar, 2020]

(Tidal-induced)
Quadrupole moment

Companion's tidal field

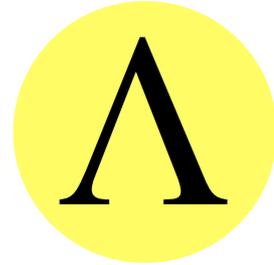
Tidal deformability
1) affects GW phase, 2) characterizes compact objects

Binary tidal deformability

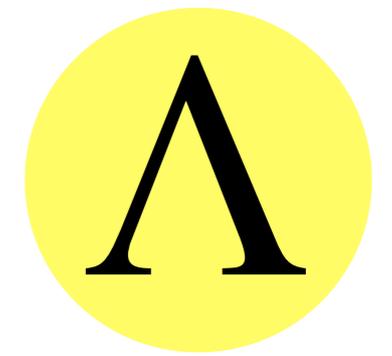
$$\tilde{\Lambda} = \frac{16}{13} [(1 + 11X_2)X_1^4\Lambda_1 + (1 \leftrightarrow 2)]$$

[Flanagan, Hinderer, 2007;
Hinderer 2008;
Vines, Flanagan, Hinderer 2011]

$\Lambda_{1,2} = \lambda_{1,2}/m_{1,2}^5$: individual ones
 $X_{1,2} = m_{1,2}/(m_1 + m_2)$: mass ratio



Tidal deformability for different EOCs



$$Q_{ij} = -\lambda \mathcal{E}_{ij}$$

$$\Lambda_{1,2} = \lambda_{1,2}/m_{1,2}^5$$

$\Lambda = 0$: BH in GR

(Schwarzschild BH [Binnington, Poisson, 2009; Damour, Nagar, 2009],

Kerr BH [Poisson, 2015; Pani+, 2015; Landry, Poisson, 2015]),

$\Lambda \sim 100 - 1000$: Neutron Stars (NSs) [Lattimer, Prakash2004].

($\Lambda < 900$ by GW170817 [LVC 2018, Narikawa+2019])

$\Lambda \neq 0$: Exotic compact objects (ECOs),

boson stars, gravastars, wormhole, quantum correction to BH

For gravastars, $\Lambda < 0$. [Uchikata, Yoshida, Pani, 2016]

Previous works: focusing on only Λ

Tidal tests: Johnson-McDaniel+, 2020 (Constraints on Boson stars by future observations of binary ECOs)

Spin-induced quadrupole moment (SIQM)

Deformation due to compact object's spin



$$Q = - (1 + \delta\kappa) \chi^2 m^3$$

$\delta\kappa = 0$: BH [Poisson, 1998],

$\delta\kappa \sim 2 - 20$: spinning NS [Laarakkers, 1997; Pappas, 2012],

$\delta\kappa \sim 10 - 150$: **spinning boson stars** [Ryan 1997],

For gravastar $\delta\kappa < 0$ is possible [Uchikata+2016].

The leading effect on GW:

symmetric combination of SIQM parameters $\delta\kappa_{1,2}$: $\delta\kappa_s = (\delta\kappa_1 + \delta\kappa_2)/2$

Previous works: focusing on only $\delta\kappa$

SIQM tests: ① Krishnendu+, 2019 (GW151226 and GW170608);

② LVK, “O3a Tests of GR” (GWTC-2 events); “O3b Tests of GR” (GWTC-3 events)

Post-Newtonian GW phase

PN phase can efficiently describe the GW emission in the inspiral regime.

PN approximation: solve the Einstein eqs. by a series in v/c .

Newton gravity + GR correction: $\mathcal{O}((v/c)^0) + \mathcal{O}((v/c)^2) + \mathcal{O}((v/c)^3) + \dots$.

(valid for slow motion $v/c \ll 1$ and weak field $GM/Rc^2 \ll 1$. Hereafter, $c=G=1$.)

$$\Psi_{\text{ECO}}(f) = \Psi_{\text{BBH}}(f) + \Psi_{\text{SIQM}}(f) + \Psi_{\text{Tidal}}(f)$$

0-5.5PN

2-3PN

5-7.5PN

η : symmetric mass ratio
Difficult to measure well

χ_{eff} : spin
Difficult to measure well

$$\sim \mathcal{M}^{-5/3} f^{-5/3} \left[1 + a_{1\text{PN}}(\eta) x^2 + a_{1.5\text{PN}}(\eta, \chi_{\text{eff}}) x^3 \right]$$

\mathcal{M} : chirp mass

Measurable very well

$$+ a_{2\text{PN}}(\eta, \chi_i^2, \kappa_s) x^4 + \dots + a_{5\text{PN}}(\eta, \tilde{\Lambda}) x^{10} + \dots]$$

v : orbital velocity

κ : spin-induced QM
Compact objects

Λ : tidal deformability
Compact objects

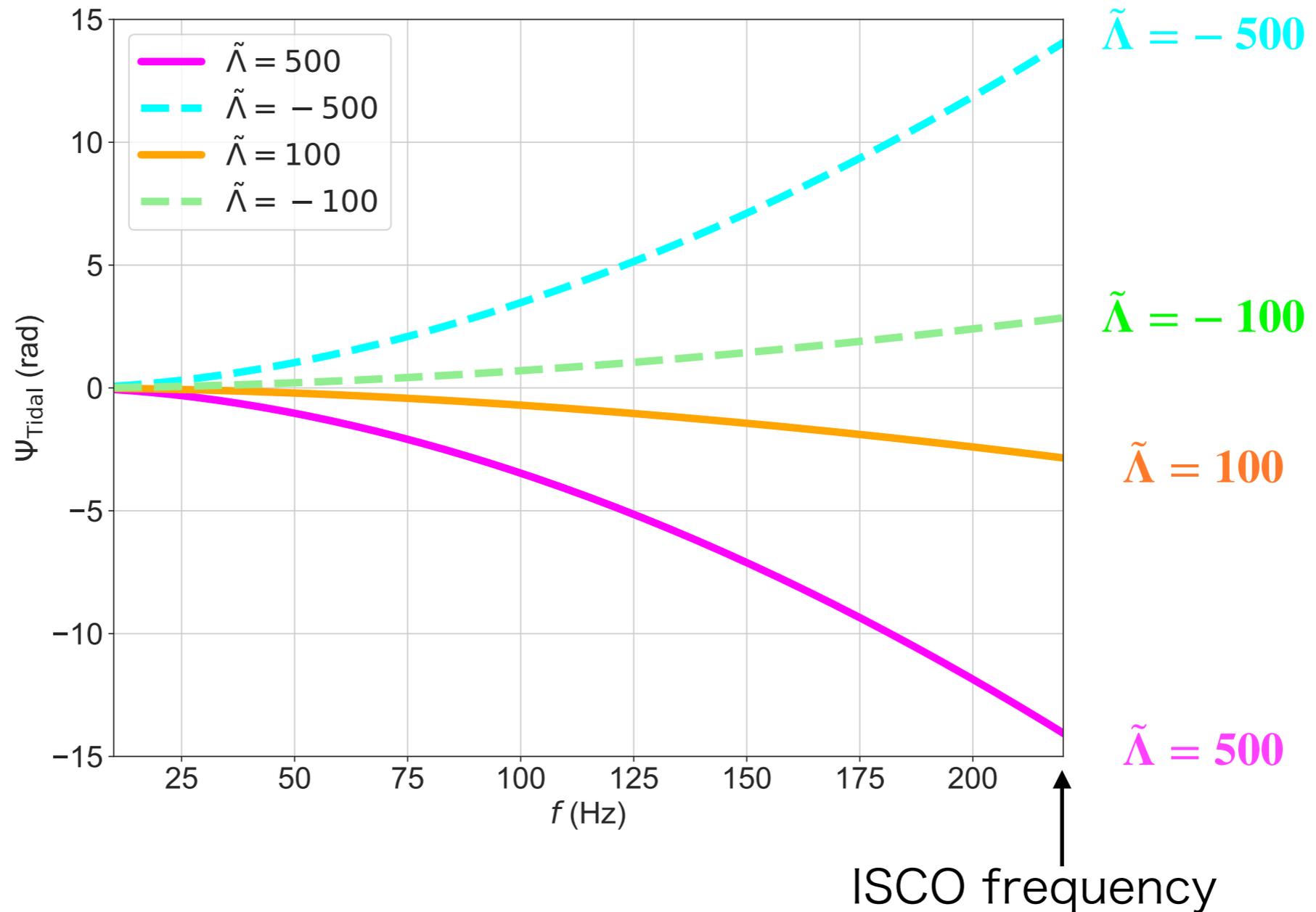
$$x = (\pi M f)^{2/3} = v^2$$

Tidal phase evolution

for unequal mass binary ECO with (12, 8) Msun

Demonstration of tidal phase evolution for binary ECO

$$a_{\text{Tidal}}^{5\text{PN}} = -\frac{39}{2}\tilde{\Lambda}$$

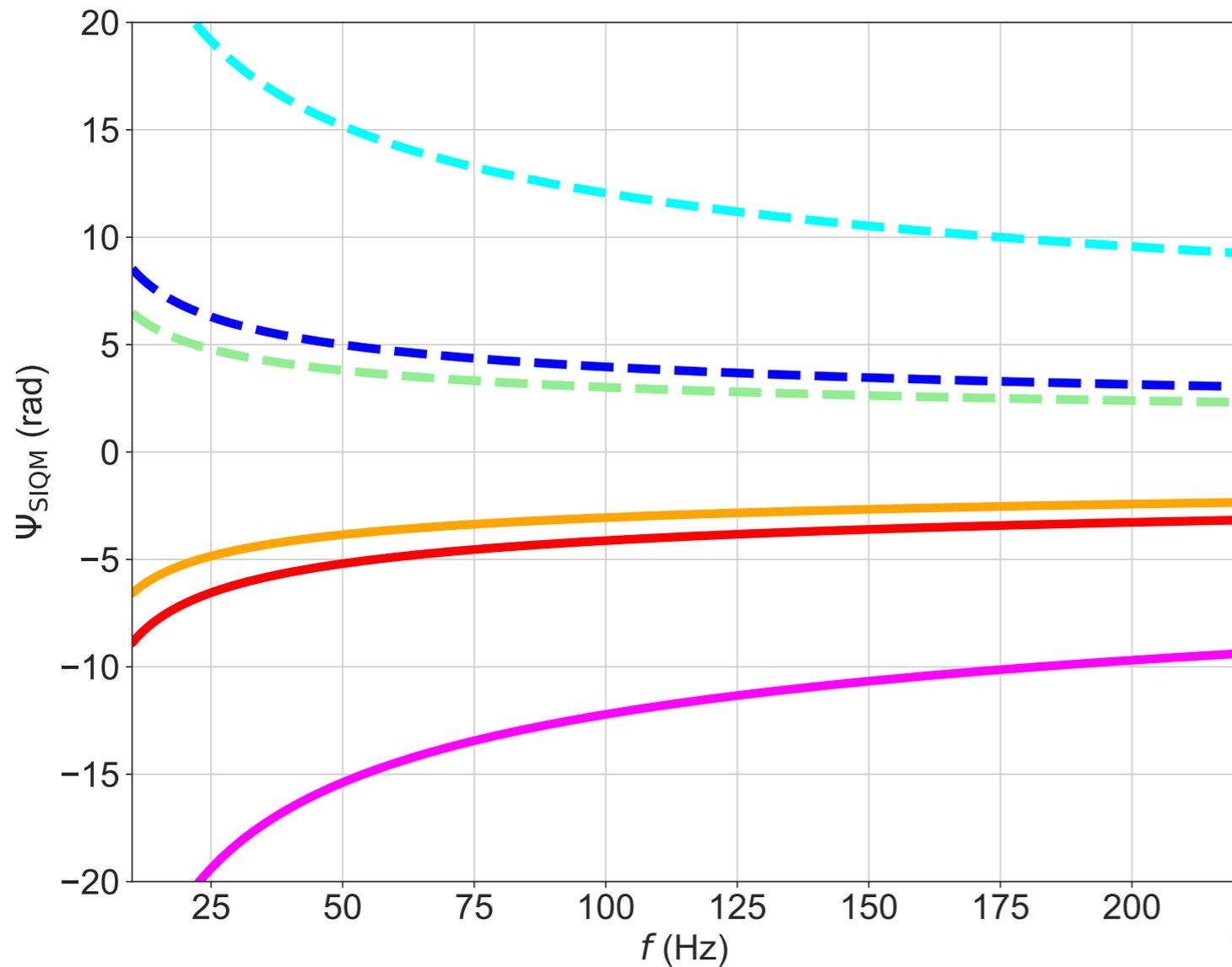


Large phase effects ~ 15 rad around ISCO frequency for $\Lambda=500$.

SIQM phase evolution

for unequal mass binary ECO with (12, 8) Msun

Demonstration of SIQM phase evolution for binary ECO



$$a_{\text{SIQM}}^{2\text{PN}} = -50\chi_s^2(1 - 2\eta)(1 + \delta\kappa_s) + \dots$$

$$\chi_{\text{eff}} = 0.1, \delta\kappa_s = -150$$

$$\chi_{\text{eff}} = 0.1, \delta\kappa_s = -50$$

$$\chi_{\text{eff}} = 0.05, \delta\kappa_s = 150$$

$$\chi_{\text{eff}} = 0.05, \delta\kappa_s = 150$$

$$\chi_{\text{eff}} = 0.1, \delta\kappa_s = 50$$

$$\chi_{\text{eff}} = 0.1, \delta\kappa_s = 150$$

ISCO frequency

Large phase effects ~ 10 rad for $\chi_{\text{eff}} = 0.1, \delta\kappa_s = 150$.

SIQM effect is strongly degenerate with spins.

Our analysis setup - parameter estimation

- Post-Newtonian (PN) inspiral waveform model:

$$\text{ECO} = \text{BBH} + \text{Tidal} + \text{SIQM}$$

$$\Lambda \quad \delta\kappa$$

- Bayesian inference library: Nested sampling in [LALSUITE \(LALInferenceNest\)](#)

Bayes's theorem

$$p(\theta|d) = \frac{\mathcal{L}(d|\theta)\pi(\theta)}{\mathcal{Z}},$$

d: data

$$\theta = \{m_1, m_2, \Lambda, \delta\kappa, \dots\}$$

Likelihood

$$\mathcal{L}(d|\theta) \propto \exp\left[-\frac{\langle d - h(\theta) | d - h(\theta) \rangle}{2}\right]$$

$$\tilde{h}(f) = \mathcal{A}(f)e^{i\Psi(f)}$$

Noise-weighted inner product

$$\langle a|b \rangle := 4\text{Re} \int_{f_{\text{low}}}^{f_{\text{high}}} df \frac{\tilde{a}^*(f)\tilde{b}(f)}{S_n(f)},$$

Evidence

$$\mathcal{Z} = \int d\theta \mathcal{L}(d|\theta)\pi(\theta).$$

Bayes factor

$$\text{BF}_{\text{BBH}}^{\text{ECO}} = \frac{\mathcal{Z}_{\text{ECO}}}{\mathcal{Z}_{\text{BBH}}}.$$

- Priors: uniform on $\tilde{\Lambda}$ and $\delta\tilde{\Lambda}$ for tidal, uniform on $\delta\kappa_{1,2}$ for SIQM.

Selected events from GWTC-2 events

Low-mass events (long inspiral):
higher cutoff frequency ≥ 120 Hz
and larger inspiral SNR ≥ 9

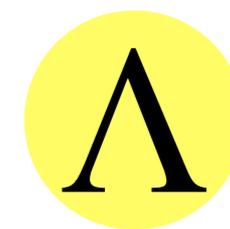
f_{high} denotes the cutoff frequency divide the inspiral and post-inspiral regimes.

Event	f_{high} [Hz]	SNR _{inspiral}
GW151226	150	10.7
GW170608	180	14.7
GW190707	160	11.2
GW190720	125	9.3
GW190728	160	12.1
GW190924	175	11.4

← the loudest
inspiral SNR

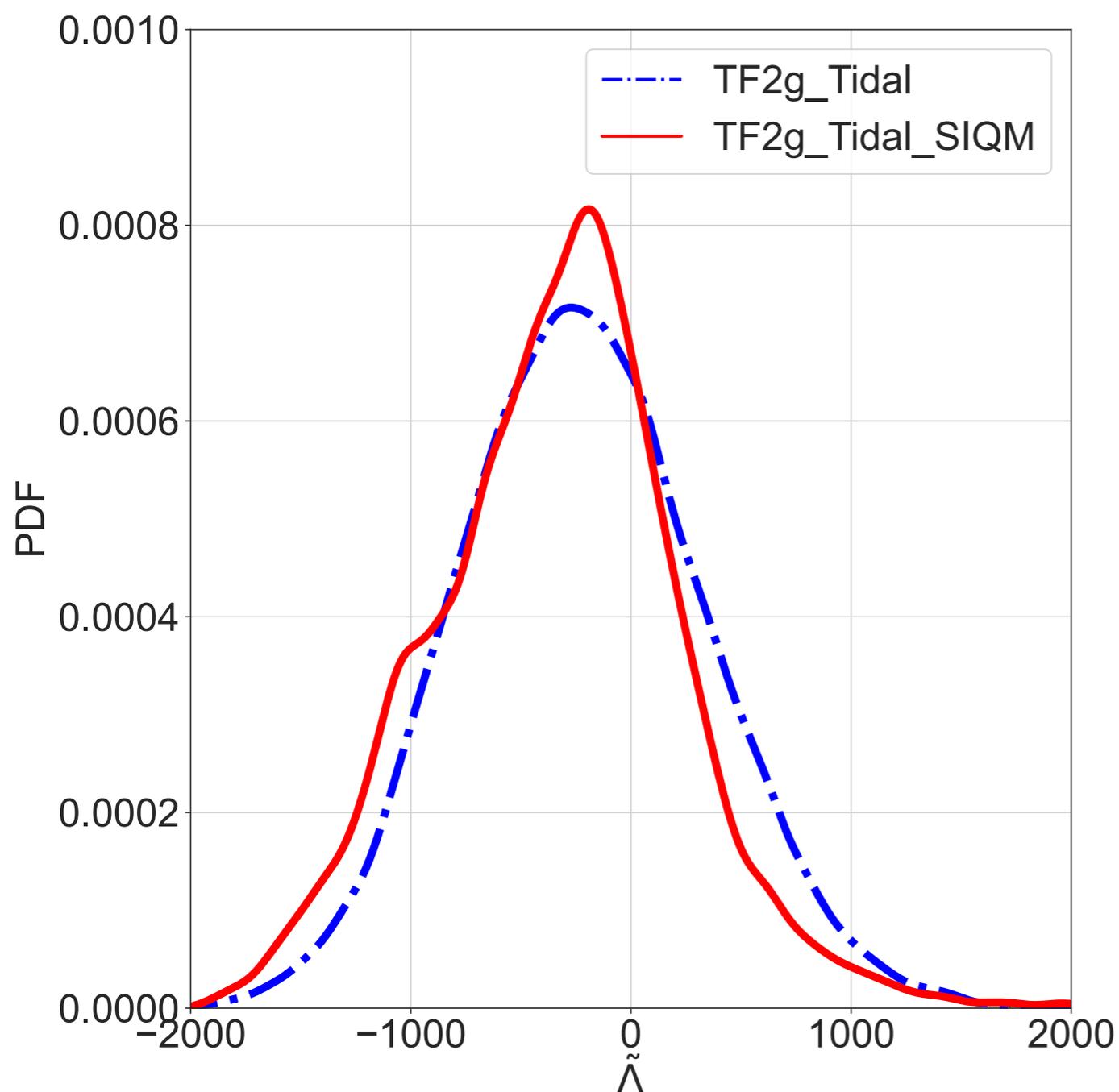
First, we present the results for GW170608 in detail.

Constraints on Tidal: GW170608



The posterior PDF of $\tilde{\Lambda}$

$f_{\text{high}}=180$ Hz



Consistent with GR ($\tilde{\Lambda} = 0$)
at the 90% CL

Adding the SIQM terms do
not affect the constraint on
the tidal deformability $\tilde{\Lambda}$.

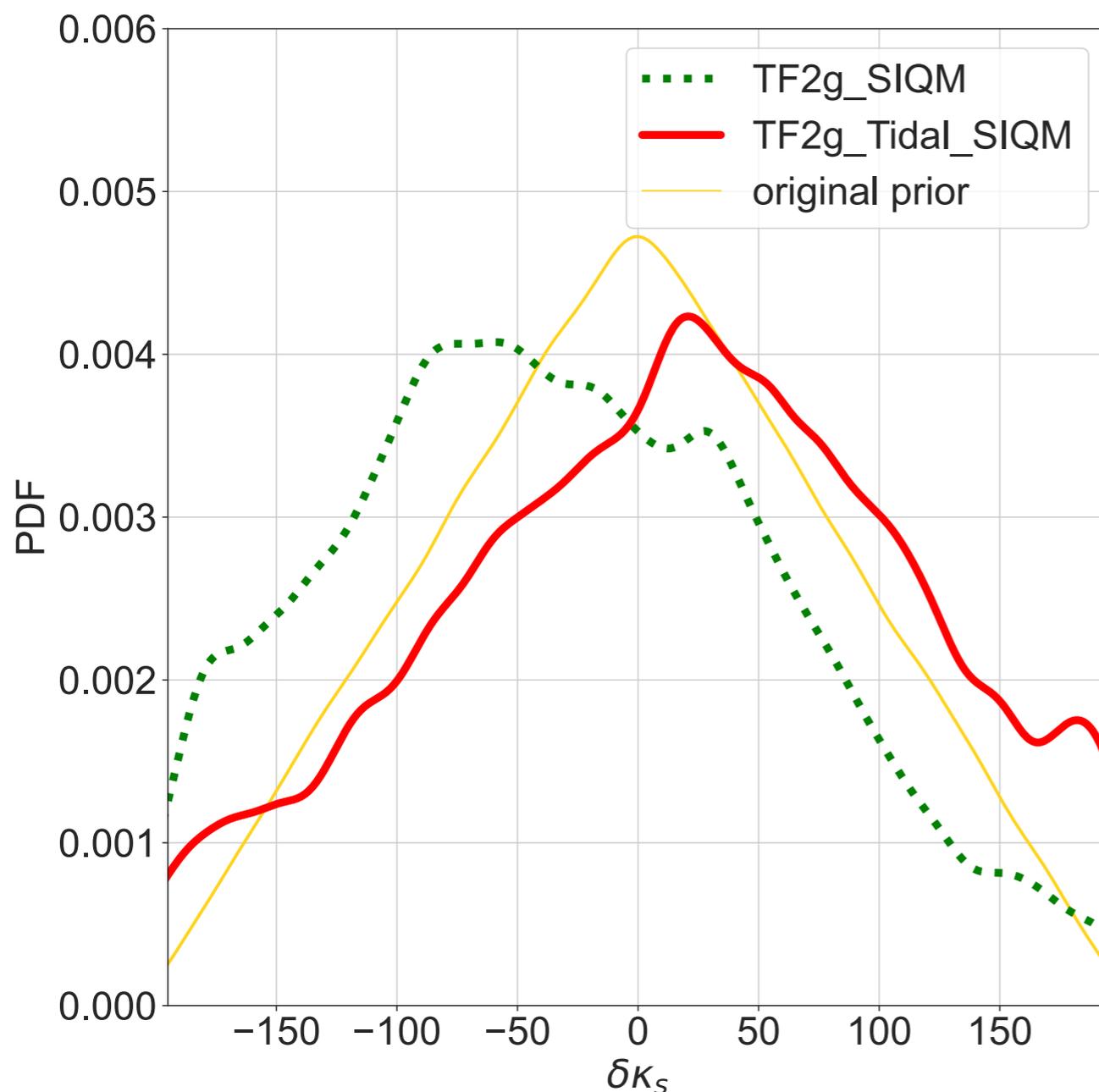
The 90% symmetric credible range
of $\tilde{\Lambda}$: [-1265, 565]

Constraints on SIQM: GW170608



The posterior PDF of $\delta\kappa_s$

$f_{\text{high}}=180$ Hz



Consistent with GR
($\delta\kappa_s = 0$) at the 90% CL

$\delta\kappa_s$ is poorly constrained for both waveform templates, which is consistent with the results shown in the previous studies by LIGO-Virgo.

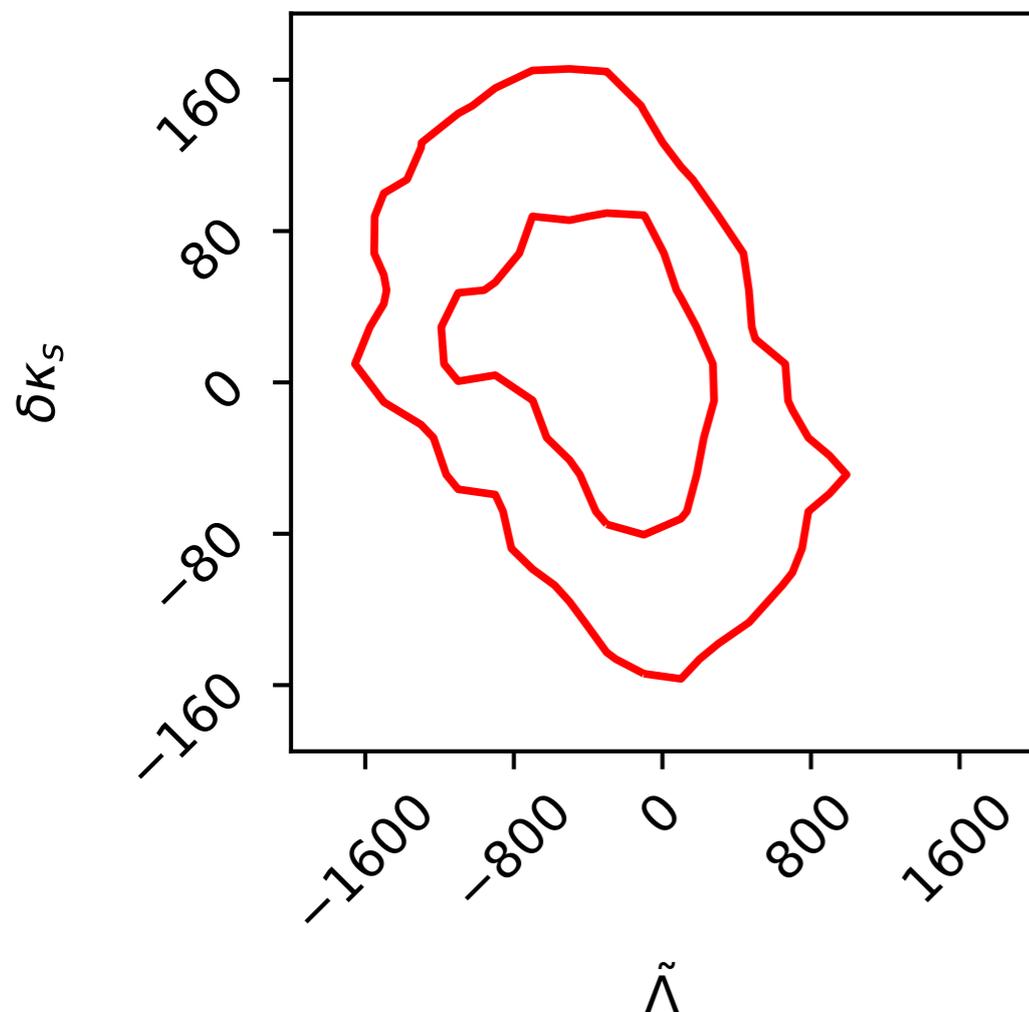
They are weighted by dividing the original prior: uniform on $\delta\kappa_{1,2}$.

Constraints on Tidal and SIQM: GW170608

The corner plots of $\tilde{\Lambda}$ - $\delta\kappa_s$ plane. (50% and 90%)

$\tilde{\Lambda}$

$\delta\kappa$



Consistent with GR
($\tilde{\Lambda} = 0$ and $\delta\kappa_s = 0$)
at the 90% CL

We find weak negative correlation between $\tilde{\Lambda}$ and $\delta\kappa_s$.

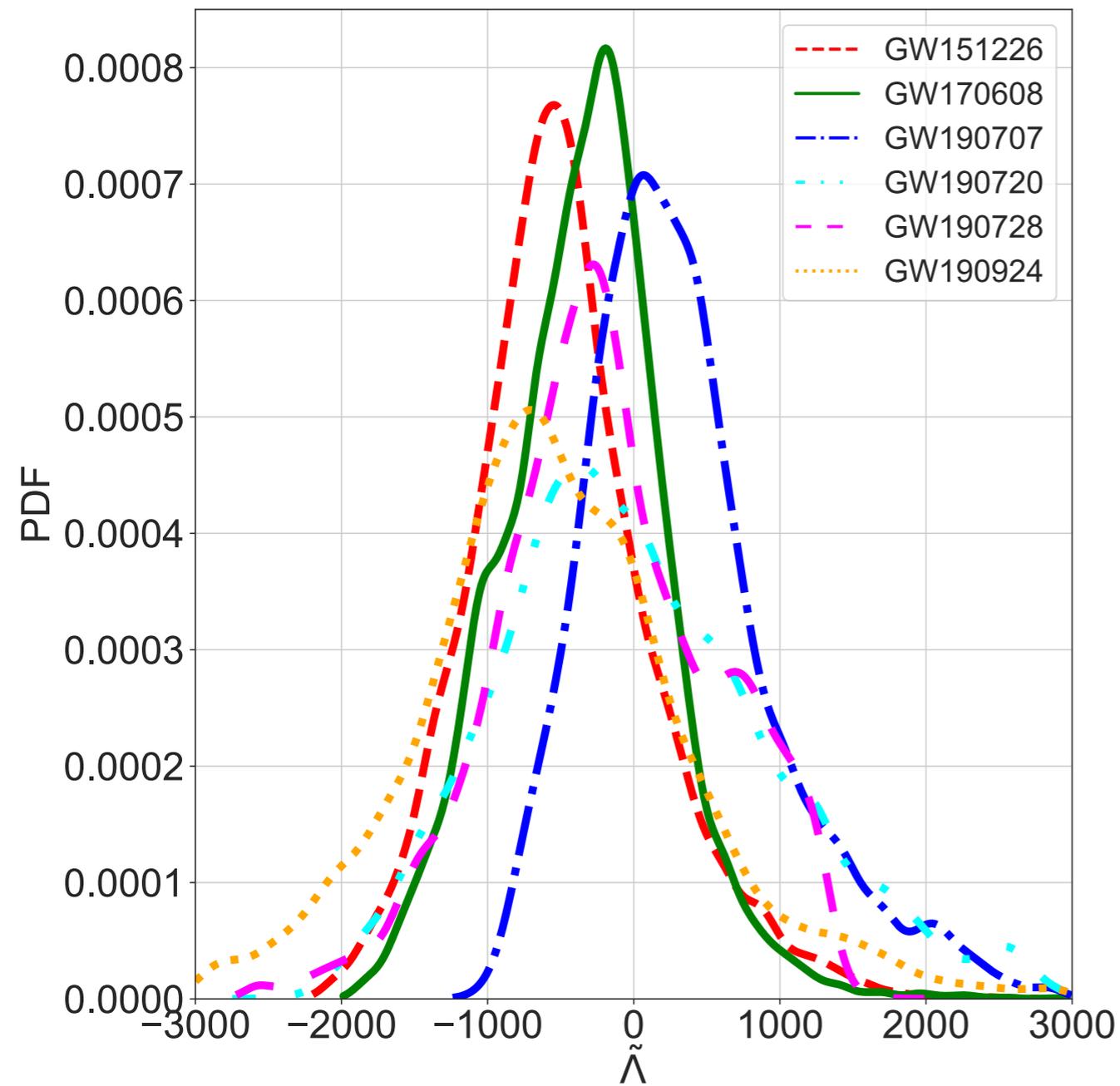
uniform priors on $\tilde{\Lambda}$, $\delta\tilde{\Lambda}$ and $\delta\kappa_{1,2}$.

— TF2g_Tidal_SIQM
 $f_{\text{high}} = 180$ Hz

Constraints on Tidal: six events



The posterior PDF of $\tilde{\Lambda}$ for six low-mass events.



All events are consistent with BBH in GR ($\tilde{\Lambda} = 0$), no evidence of deviation from GR

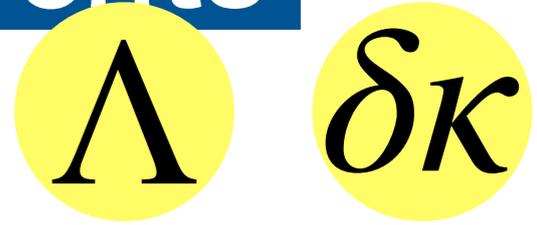
Event	$\tilde{\Lambda}$
GW151226	[-1441, 649]
GW170608	[-1265, 565]
GW190707	[-590, 1661]
GW190720	[-1445, 1768]
GW190728	[-1432, 1078]
GW190924	[-2041, 1118]

TF2g_Tidal_SIQM waveform model

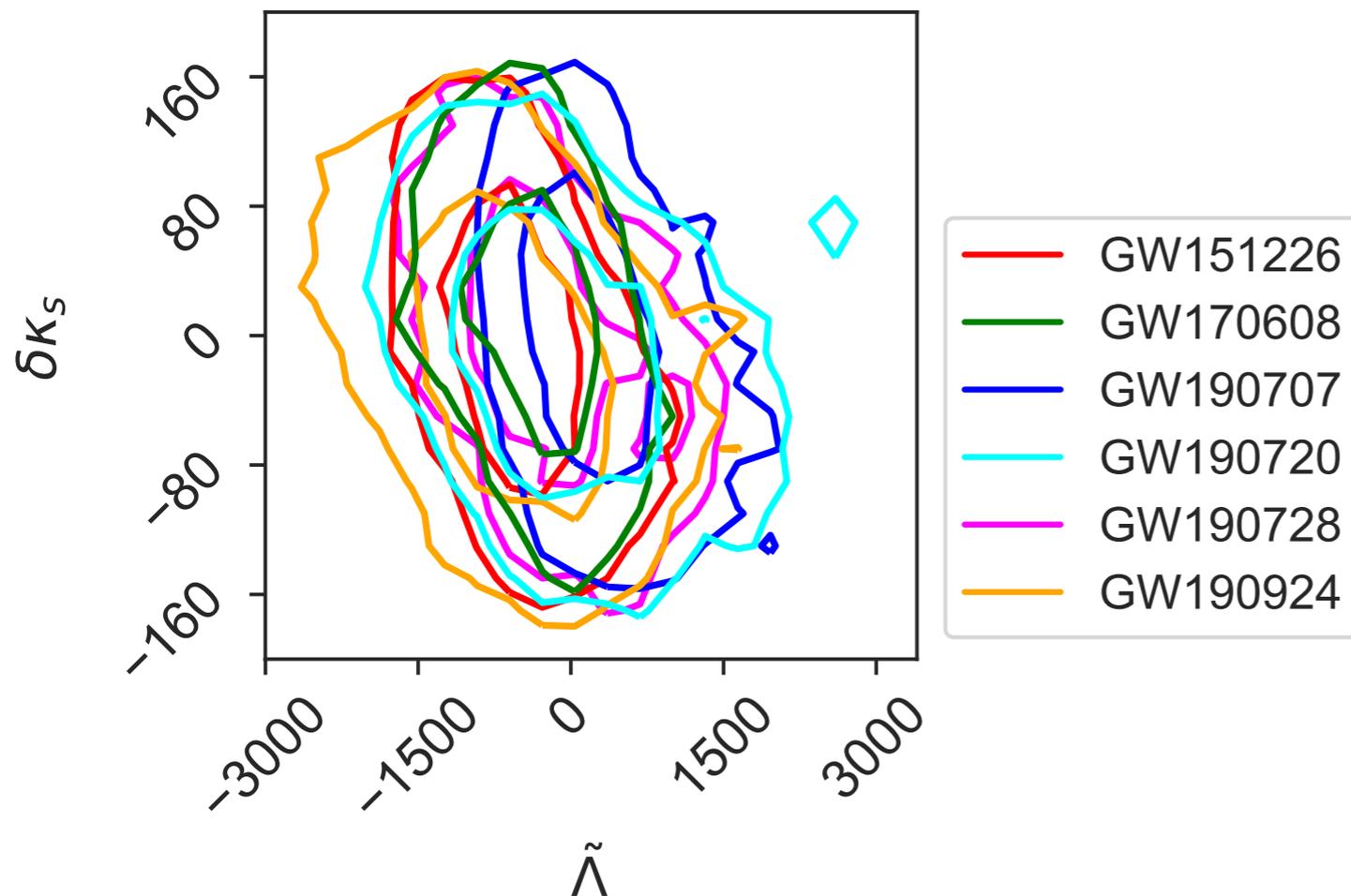
90% symmetric intervals

Constraints on Tidal and SIQM: six events

The corner plots of $\tilde{\Lambda}$ - $\delta\kappa_s$ plane for six low-mass events.



TF2g_Tidal_SIQM waveform model



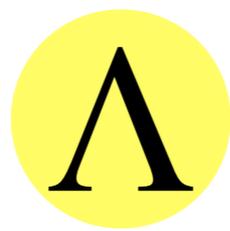
Event	$\log_{10} \text{BF}_{\text{BBH}}^{\text{ECO}}$
GW151226	-0.45
GW170608	-2.08
GW190707	-2.07
GW190720	-1.77
GW190728	-1.98
GW190924	-2.03
Combined	-10.38

All events are consistent with BBH in GR ($\tilde{\Lambda} = 0$ and $\delta\kappa_s = 0$)

We find weak negative correlation between $\tilde{\Lambda}$ and $\delta\kappa_s$.

The binary ECO model (with Tidal and SIQM) is disfavored compared to the BBH in GR.

Conclusion



- We analyzed six low-mass GWTC-2 events using the post-Newtonian waveform model.
- **The first constraints on $\tilde{\Lambda}$ of events classified as BBH**
- **We found that all events that we have analyzed are consistent with BBH mergers in GR ($\tilde{\Lambda} = 0$ and $\delta\kappa_s = 0$).**
- **The binary ECO model (with tidal and SIQM terms) is disfavored compared to the BBH in GR.**

Future work

- Results of GWTC-3 events will appear soon.